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## The Roles of Filters in Power Systems

The implementation of harmonic filters has become an essential element of electric power networks. With the advancements in technology and significant improvements of power electronic devices, utilities are continually pressured to provide high-quality and reliable energy. Power electronic devices such as computers, printers, fax machines, fluorescent lighting, and most other office equipment generate harmonics. These types of devices are commonly classified as nonlinear loads. These loads (e.g., rectifiers, inverters) create harmonics by drawing current in short pulses rather than in a sinusoidal manner.

Harmonic currents and the associated harmonic powers must be supplied from the utility system. The major issues associated with the supply of harmonics to nonlinear loads are severe overheating: increased operating temperatures of generators and transformers degrade the insulation material of their windings. If this heating were continued to the point at which the insulation fails, a flashover would occur. This would partially or permanently damage the device and result in loss of generation or transmission that could cause blackouts. Impacts of harmonics on the insulation of transformers and electrical machines are discussed in Chapter 6.

One solution to this problem is to install a harmonic filter for each nonlinear load connected to the power system. There are different types of harmonic filters including passive, active, and hybrid configurations [1-8]. The installation of active filters proves indispensable for solving power quality problems in distribution networks such as the compensation of harmonic current and voltage, reactive power, voltage sags, voltage flicker, and negative-phase sequence currents. Ultimately, this would ensure a system with increased reliability and better power quality.

Filters can only compensate harmonic currents and/or harmonic voltages at the installed bus and do not consider the power quality of other buses. On the other hand, as the number of nonlinear loads increases, more harmonic filters are required. New generations of active filters are unified power quality conditioners (UPQCs) and active power line

conditioners (APLCs). The UPQCs are discussed in Chapter 11.

This chapter begins with a discussion of the different types of nonlinear loads. Section 9.2 presents a broad classification of filters as they are employed in supply systems, and thereafter the subclassification of filters according to their topology. The next three sections focus on different types of filter topologies including passive, active, and hybrid configurations. Block diagrams of active filters are reviewed in Section 9.6. Detailed discussion and classification of control methods for active and hybrid filters are presented in Section 9.7. The chapter ends with general comments and conclusions.

### 9.1 TYPES OF NONLINEAR LOADS

There are three main types of nonlinear loads in power systems: current-source loads, voltage-source loads, and their combinations.

The first category of nonlinear loads includes the current-source (current-fed or current-stiff) loads. Traditionally, most nonlinear loads have been represented as current sources because their current waveforms on the AC side are distorted. Examples of this category include the phase-controlled thyristor rectifier with a filter inductance on the DC side of the rectifier resulting in DC currents (Fig. 9.1); thyristor rectifiers convert an AC voltage source to a DC current source supplying current-source inverters (CSIs) and high-voltage DC (HVDC) systems, and diode rectifiers with sufficient filter inductance supply DC loads. In general, highly inductive loads are served by silicon-controlled rectifiers (SCRs) converting AC power to DC power. Of course, the inverse operation - where an inverter supplies AC power from a DC power source - results in similar current distortions (e.g., harmonics) on the AC side of the inverter. The transfer characteristics and resulting harmonic currents of current-source nonlinear loads are less dependent on the circuit parameters of the AC side than those on the DC side. Accordingly, passive shunt, active shunt, or hybrid (e.g., a combination of active shunt in series

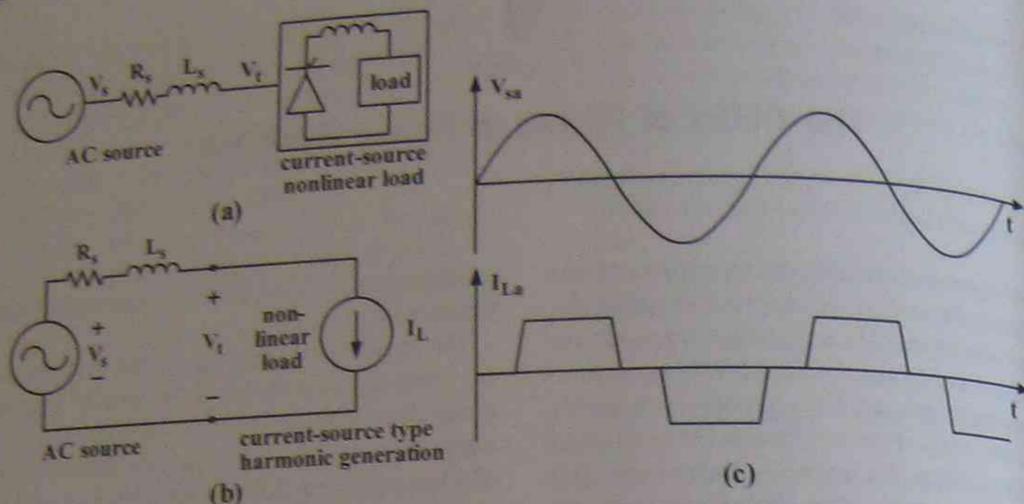


FIGURE 9.1 Typical current-source nonlinear load: (a) thyristor rectifier for DC drives, (b) per-phase equivalent circuit of thyristor rectifier, (c) typical phase-voltage and line-current waveforms of thyristor rectifier.

with passive shunt) filters for harmonic compensation are commonly applied on the AC side of the converters serving nonlinear loads. The principle of the passive shunt filter is to provide a low-impedance shunt branch for the harmonic currents caused by the nonlinear load. These passive filters have been applied in Chapter 1. The principle of the active shunt filter is to inject into the power system harmonic currents with the same amplitudes and opposite phases of the harmonic currents due to nonlinear loads, thus eliminating harmonic current flowing into the AC source.

The second category of nonlinear loads comprises voltage-source (or voltage-fed or voltage-stiff) loads, such as diode rectifiers with a capacitive filter at the DC link feeding variable-frequency voltage-source inverter (VSI)-based AC motor drives, power supplies with front-end diode rectifier and capacitive filters installed in computers and other household appliances, battery chargers, etc. These voltage-stiff loads draw discontinuous and nonsinusoidal currents resulting in very high THD<sub>i</sub>, low power factor, and distortions of the AC terminal voltage at the point of common coupling (PCC) defined in Chapter 1. These loads generate harmonic voltage sources, rather than harmonic current sources (Fig. 9.2). Their harmonic amplitudes are greatly affected by the AC side impedance and source voltage imbalance, whereas their rectified voltages are less dependent on the impedance of the AC system. Therefore, diode rectifiers behave like a voltage source, rather than a current source. Accordingly, passive series, active series, or hybrid (e.g., a combination of active

series with passive series) filters are relied on to compensate distortions due to nonlinear loads. Current-source and voltage-source nonlinear loads exhibit dual relations to one another with respect to circuits and properties, and can be effectively compensated by parallel and series filters discussed in Chapter 1, respectively [1].

The third category of nonlinear loads is characterized by the combination of current- and voltage-source loads. They are neither of the current-source nor of the voltage-source type and may contain loads of both kinds. For example, adjustable-speed drives behave as several types of nonlinear loads; variable-frequency VSI-fed AC motors perform as voltage-stiff loads, whereas CSI-fed AC motor drives act as current-stiff loads. For these loads a hybrid topology consisting of active series with passive shunt filter elements is appropriate, provided that the power supply is ideal and adjustable reactive power compensation is not required.

The assessment of harmonic injection of nonlinear loads may not be easy and depends on the following [4]:

- type and topology of nonlinear loads producing harmonics. A voltage-source converter with diode front end may inject an entirely different harmonic spectrum as compared with a current-source converter. Switching power supplies, pulse-width-modulation (PWM) drives, cycloconverters, and arc furnaces have their own specific harmonic spectra;
- interaction of nonlinear loads with the AC system impedance; and

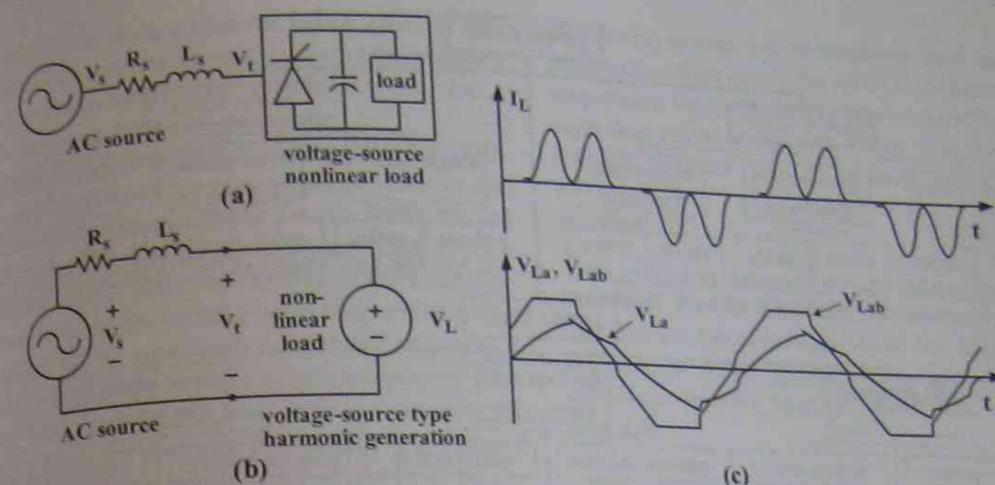


FIGURE 9.2 Typical voltage-source nonlinear load: (a) diode rectifier for AC drives, electronic equipment, etc., (b) per-phase equivalent circuit of diode rectifier, (c) typical line-current and phase and line-to-line voltage waveforms of thyristor rectifier.

- the harmonic spectra may vary as a function of the nonlinear load. For example, the input AC waveform to a current-source converter and its ripple content depends on the firing angle  $\alpha$  and the length of the commutation interval – due to the commutating inductance – as pointed out in Chapter 1. In addition, a small amount of noncharacteristic harmonics may be generated. Therefore, worst-case scenarios should be considered for the analyses of these load types.

## 9.2 CLASSIFICATION OF FILTERS EMPLOYED IN POWER SYSTEMS

During the past few decades the number and types of nonlinear loads have tremendously increased. This has motivated the utilities and consumers of electric power to implement different harmonic filters. Filters are capable of compensating harmonics of nonlinear loads through current-based compensation. They can also improve the quality of the AC supply, for example, compensating voltage harmonics, sags, swells, notches, spikes, flickers, and imbalances through voltage-based techniques. Filters are usually installed near or close to the points of distortion, for example, across nonlinear loads, to ensure that harmonic currents do not interact with the power system. They are designed to provide a bypass for the harmonic currents, to block them from entering the power system, or to compensate them by locally supplying harmonic currents and/or harmonic voltages.

Filters can be designed to trap harmonic currents and shunt them to ground through the use of capacitors, coils, and resistors. Due to the lower impedance of a filter element (at a certain frequency) in comparison to the impedance of the AC source, harmonic currents will circulate between the load and the filter and do not affect the entire system; this is called series resonance as defined in Chapter 1. A filter may contain several of these filter elements, each designed to compensate a particular harmonic frequency or an array of frequencies. Filters are often the most common solution approaches that are used to mitigate harmonics in power systems. Unlike other solutions, filters offer a simple and inexpensive alternative with high benefits.

Classifications of filters may be performed based on various criteria, including the following:

- number and type of elements (e.g., one, two, or more passive and/or active filters),
- topology (e.g., shunt-connected, series-connected, or a combination of the two),
- supply system (e.g., single-phase, three-phase three-wire, and three-phase four-wire),
- type of nonlinear load such as current-source and/or voltage-source loads,
- power rating (e.g., low, medium, and high power),
- compensated variable (e.g., harmonic current, harmonic voltage, reactive power, and phase balancing, as well as multiple compensation).

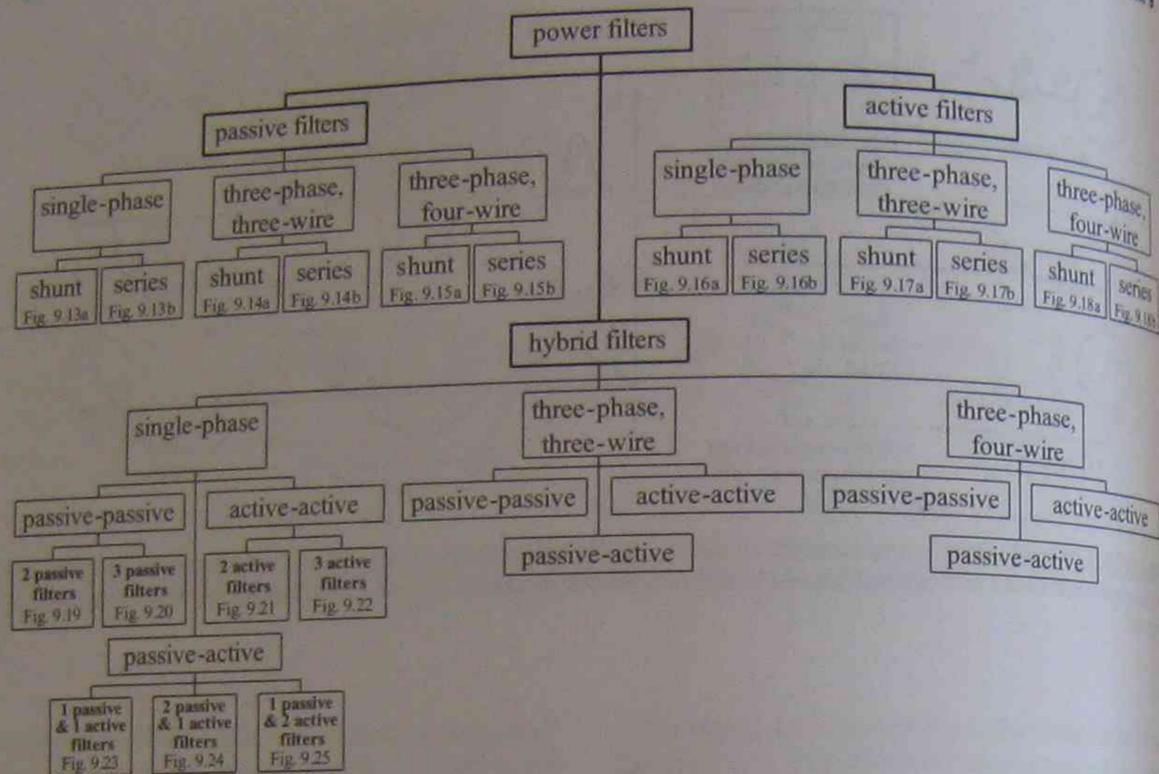


FIGURE 9.3 Classification of filters used for power quality improvement [1–5].

- converter type (e.g., VSI and/or CSI to realize active elements of filter),
- control technique (e.g., open loop, constant capacitor voltage, constant inductor current, linear voltage control, or optimal control), and
- reference estimation technique (e.g., time and/or frequency current/voltage reference estimation).

Various topologies such as passive filter (PF), active filter (AF), and hybrid filter (HF) in shunt, series, and shunt/series for single-phase, three-phase three-wire, and three-phase four-wire systems have been installed using current-source inverters and voltage-source inverters for implementation of the control of active filters. Figure 9.3 shows the classification of filters as used in power systems based on the supply system with the topology as a subclassification [1–5]. Further classification is made on the basis of the numbers and types of elements employed in different topologies. According to Fig. 9.3, there are 156 valid configurations of passive, active, and hybrid filters. Each class of filters offers its own unique solution to improve the quality of electric power. The choice of filter depends on the nature of the power quality problem, the required level and speed of compensation, as well as the economic cost associated with its implementation.

### 9.3 PASSIVE FILTERS AS USED IN POWER SYSTEMS

If a nonlinear load is locally causing significant harmonic distortion, passive filters may be installed to prevent the harmonic currents from being injected into the system. Passive filters are inexpensive compared with most other mitigating devices. They are composed of only passive elements (inductances, capacitances, and resistances) tuned to the harmonic frequencies of the currents or voltages that must be attenuated. Passive filters have better performances when they are placed close to the harmonic-producing nonlinear loads. They create a sharp parallel resonance at a frequency below the notch (tuned) frequency as introduced in Chapter 1. The resonant frequency of the power system must be carefully placed far from any significant harmonic distortion caused by the nonlinear load. For this reason, passive filters should be tuned slightly lower than the harmonic to be attenuated. This will provide a margin of safety in case there is some change in the system parameters. Otherwise, variations in either filter capacitance and/or filter inductance (e.g., with temperature or failure) might shift resonance conditions such that harmonics cause problems in the power system. In practice, passive filters are added

to the system starting with the lowest order of harmonics that must be filtered; for example, installing a seventh-harmonic filter usually requires that a fifth-harmonic filter also be included.

There are various types of passive filters for single-phase and three-phase power systems in shunt and series configurations. Shunt passive filters are the most common type of filters in use. They provide low-impedance paths for the flow of harmonic currents. A shunt-connected passive filter carries only a fraction of the total load current and will have a lower rating than a series-connected passive filter that must carry the full load current. Consequently, shunt filters are desirable due to their low cost and fine capability to supply reactive power at fundamental frequency. It is possible to use more than one passive filter in either shunt and/or series configuration. These topologies are classified as passive-passive single- and three-phase hybrid filters (Fig. 9.3) and will be discussed in Section 9.5. The structure chosen for implementation depends on the type of the dominant harmonic source (voltage source, current source) and the required compensation function (e.g., harmonic current or voltage, reactive power).

distribution system with a nonlinear load and a passive shunt filter installed at the PCC. At harmonic frequencies, the system can be approximated by the equivalent circuit of Fig. 9.4b. Three main types of transfer functions can be defined: impedance, current-divider, and voltage-divider transfer functions.

**Impedance Transfer Functions.** Impedance transfer functions are the most basic blocks for design and modeling of power systems. Two types of filter impedance transfer functions have been defined (Fig. 9.4):

- **Filter impedance transfer function** is the impedance frequency response of the filter expressed in the  $s$  domain as

$$H_f(s) = Z_f(s) = \frac{V_f(s)}{I_f(s)} \quad (9-1a)$$

where  $Z_f(s)$ ,  $V_f(s)$ , and  $I_f(s)$  are the filter impedance, complex voltage, and current, respectively, and  $s = j\omega$  is the Laplace operator.

- **Filter system impedance transfer function** is defined after the filter is designed and connected to the network. It is the impedance frequency response of the system (with the filter installed) expressed in the  $s$  domain:

#### 9.3.1 Filter Transfer Function

Transfer functions are extensively used for filter design and system modeling. Figure 9.4a shows the single-phase presentation of a balanced three-phase

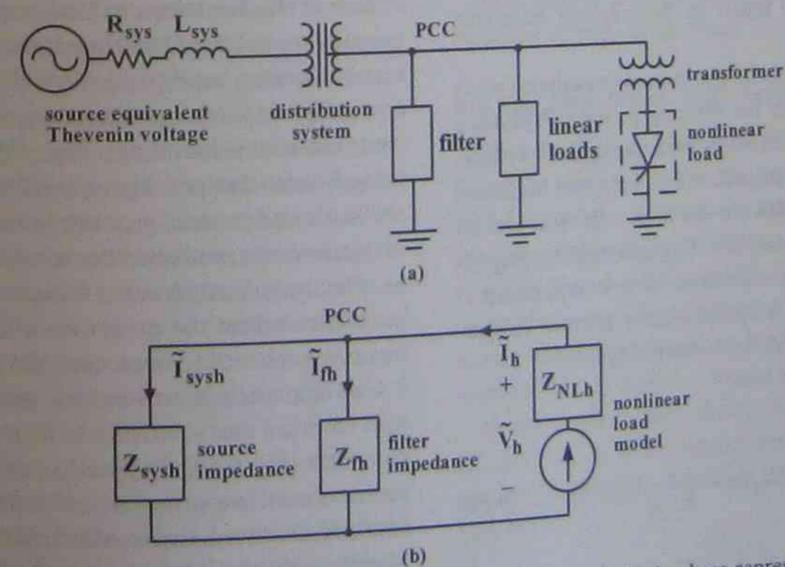


FIGURE 9.4 Distribution system with nonlinear load and passive shunt filter; (a) single-phase representation, (b) equivalent circuit for harmonic (of order  $h$ ) filter installation, see Chapter 1.

$$H_{f_{sys}}(s) = Z_{f_{sys}}(s) = \frac{V_{sys}(s)}{I_f(s) + I_{sys}(s)} = \frac{1}{\frac{1}{Z_f(s)} + \frac{1}{Z_{sys}(s)}} \quad (9-1b)$$

where  $Z_{f_{sys}}(s)$  is the impedance of the system after the connection of the filter and  $V_{sys}(s)$  and  $I_{sys}(s)$  are the system complex voltage and current, respectively.

**Current-Divider Transfer Functions.** Two types of current-divider transfer functions are derived for a filter (Fig. 9.4):

- $H_{cds}(s)$  is the ratio of system (sys) harmonic current to the injected harmonic nonlinear (NL) current:

$$H_{cds}(s) = \frac{I_{sys}(s)}{I_{NL}(s)} = \frac{Z_f(s)}{Z_f(s) + Z_{sys}(s)} = \rho_{sys}(s) \quad (9-2a)$$

- $H_{cdf}(s)$  is the ratio of filter (f) harmonic current to injected harmonic nonlinear current:

$$H_{cdf}(s) = \frac{I_f(s)}{I_{NL}(s)} = \frac{Z_{sys}(s)}{Z_f(s) + Z_{sys}(s)} = \rho_f(s) \quad (9-2b)$$

In Eqs. 9-2,  $\rho_{sys}(s)$  and  $\rho_f(s)$  are complex quantities that determine the distribution of the harmonic currents in the filter and the system and have been introduced in Chapter 1. A properly designed filter will have  $\rho_f(s)$  close to unity, typically 0.995, and  $\rho_{sys}(s)$  about 0.045 with the corresponding angles of about 2.6° and 81°, respectively. It is desirable that  $\rho_{sys}(s) = \rho_{sys}(j\omega)$  be small at the various occurring harmonics.

According to Eqs. 9-2 the system impedance plays an important role in the filtering process. Without a filter, all harmonic currents pass through the system. For a large system impedance and a given harmonic frequency, the bypass via the filter is perfect and all current harmonics will flow through the filter impedance. Conversely, for a system of low impedance at a given harmonic frequency most current of harmonic frequency will flow into the system.

It is easy to show that

$$H_{cdf}(s) = \frac{Z_{sys}(s)}{Z_f(s)} H_{cds}(s) = \frac{1}{Z_f(s)} H_{f_{sys}}(s), \quad (9-3a)$$

$$H_{cds}(s) = \frac{1}{Z_{sys}(s)} H_{f_{sys}}(s). \quad (9-3b)$$

When designing a filter the impedance transfer functions (Eqs. 9-1) can be used to evaluate the overall system performance. After the filter is installed, computed and measured current-divider ratios (Eqs. 9-2) can be plotted to evaluate filter performance and determine whether harmonic current distortion limits comply with the IEEE-519 Standard [11], as discussed in Chapter 1 (Application Examples 1.8 and 1.9).

**Voltage-Divider Transfer Functions.** Similar transfer functions can be developed for systems with loads that are sensitive to harmonic voltages. Filters are used to provide frequency detuning or voltage distortion control. These transfer functions are based on a voltage division between an equivalent harmonic voltage source – representing nonlinear loads – and harmonic sensitive loads. Applications of these transfer functions are concerned with the voltage distortion amplification of shunt power factor capacitors due to parallel and series resonances.

### 9.3.2 Common Types of Passive Filters for Power Quality Improvement

The configuration of a filter depends on the frequency spectrum and nature of the distortion. Figure 9.5 depicts common types of passive filters.

The first-order damped and undamped high-pass filter (Fig. 9.5a with and without the resistor, respectively) is used to attenuate high-frequency current harmonics that cause telephone interference, reduce voltage notching caused by commutation of SCRs, and provide partial displacement power factor correction of the fundamental load current. The single-tuned low-pass (also called band-pass or second-order series resonant band-pass) filter (Fig. 9.5b) is most commonly applied for mitigation of a single dominant low-order harmonic. Fig. 9.5c represents a second-order damped high-pass filter. Most nonlinear loads and devices generate more than one harmonic, however, and one filter is not usually adequate to effectively compensate, mitigate, or reduce all harmonics within the power system. There are different approaches to overcome this problem.

One approach is to use two single-tuned filters with identical characteristics to form a double band-pass filter (Fig. 9.5d). In practice, there is more than one dominant low-order harmonic and combinations of three or more single-tuned filters are applied. Starting with the lowest harmonic order (e.g., 5th), each filter is tuned to one harmonic frequency. This approach is not practical when the number of domi-

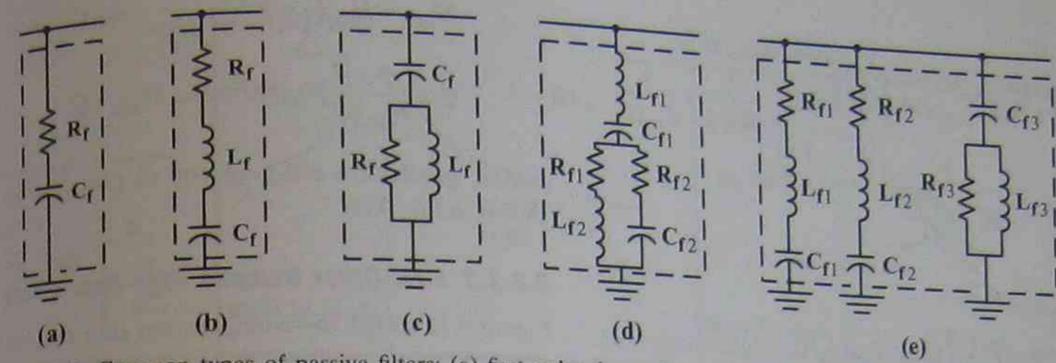


FIGURE 9.5 Common types of passive filters; (a) first-order damped high-pass filter, (b) second-order series resonant band-pass filter, (c) second-order damped high-pass filter, (d) fourth-order double band-pass filter, (e) composite filter consisting of two band-pass filters and one high-pass filter.

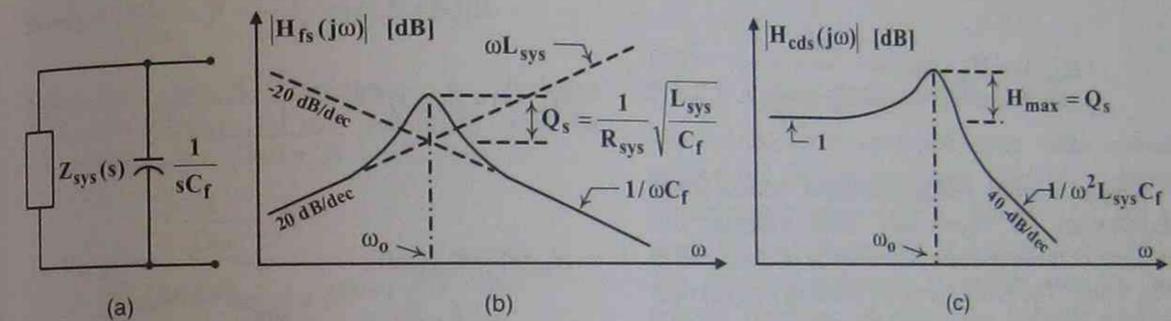


FIGURE 9.6 First-order high-pass filter; (a) equivalent circuit, (b) filter system impedance transfer function, (c) current-divider transfer function.

nant low-order harmonics is large and/or higher order harmonics are present.

Another approach is to use a first-order high-pass filter (consisting of a resistor connected in series with a capacitor) or a second-order high-pass filter (consisting of a series capacitor and a parallel combination of inductor and resistor; Fig. 9.5c) and set the resonant frequency below the lowest order dominant harmonic frequency. However, the  $Z - \omega$  plot of a second-order high-pass filter shows that the minimum impedance of this filter (e.g., in the pass-band region) is higher than that of a single-tuned band-pass filter. Therefore, the high-pass filter allows a percentage of all harmonics above its notch frequency to pass through and will result in large fundamental filter rating and high resistive losses. This filter is commonly applied for higher frequencies and notch reduction.

The third and most implemented approach is to install a composite filter consisting of two or more branches of band-pass filters tuned at low-order harmonic frequencies and a parallel branch of high-pass filter tuned at higher frequencies (called a passive filter element; Figs. 9.5e, 9.11, and 9.12). This con-

figuration is suitable for most residential, domestic, and industrial nonlinear loads such as arc furnaces. In addition, there are other configurations of higher order filters (e.g., third-order damped filter) for transmission systems.

This section derives the equations and general relations of basic filter types.

#### 9.3.2.1 First-Order, High-Pass Filter

A first-order, high-pass filter consists of a shunt capacitor (Fig. 9.6a) and can be used to attenuate high-frequency harmonic current components causing telephone interference, to reduce voltage notching (e.g., caused by rectifier commutation), and to improve the displacement (fundamental) load power factor. Such filters are amply described in currently available circuit textbooks [12, 13].

If the system impedance is purely inductive ( $Z_{sys}(s) = sL_{sys}$ ), filter impedance and filter system impedance transfer functions can be derived using Eqs. 9-1:

$$H_f(s) = Z_f(s) = \frac{V_f(s)}{I_f(s)} = \frac{1}{sC_f} \quad (9-4a)$$

$$H_{f_{sys}}(s) = Z_{f_{sys}}(s) = \frac{V_{f_{sys}}(s)}{I_f(s) + I_{sys}(s)} = \frac{1}{\frac{1}{Z_f(s)} + \frac{1}{Z_{sys}(s)}} = \frac{1}{sC_f + \frac{1}{sL_{sys}}} \quad (9-4b)$$

The order of this filter, that is, the highest exponent of the characteristic (denominator) polynomial of  $H_f(s)$ , is one.

The current-divider transfer function, Eq. 9-2a, can be derived as

$$H_{cds}(s) = H_{cds}(j\omega) = \frac{\frac{1}{j\omega C_f}}{j\omega L_{sys} + \frac{1}{j\omega C_f}} \quad (9-5)$$

Simple algebra yields analytical (closed-form) expressions for asymptotes, local maxima, and minima of these transfer functions as is illustrated in Fig. 9.6b,c. The procedures for plotting  $H_{cds}(j\omega)$  on a logarithm paper as shown in Fig. 9.6c are

- For low frequencies ( $\omega \ll 1/\sqrt{L_{sys}C_f} \Rightarrow |1/j\omega C_f| \gg |j\omega L_{sys}|$ ):

$$H_{cds}(j\omega) = \frac{1}{j\omega C_f} = 1.$$

Therefore, the roll-off of the low-frequency components is one or 0 dB per decade.

- For high frequencies ( $\omega \gg 1/\sqrt{L_{sys}C_f} \Rightarrow |1/j\omega C_f| \ll |j\omega L_{sys}|$ ):

$$H_{cds}(j\omega) = \frac{1}{j\omega L_{sys}} = \frac{-1}{\omega^2 L_{sys} C_f}$$

Therefore, the roll-off of the high frequency components is  $1/\omega^2$  or -40 dB per decade.

If system resistance is included ( $Z_{sys}(s) = R_{sys} + sL_{sys}$ ), the maximum can be found as

$$H_{cds}(s = j\omega) \Big|_{\omega = \frac{1}{\sqrt{L_{sys}C_f}}} = -j \frac{1}{R_{sys}} \sqrt{\frac{L_{sys}}{C_f}}$$

and

$$H_{max} = |H_{cds}(s = j\omega) \Big|_{\omega = \frac{1}{\sqrt{L_{sys}C_f}}} \text{ with } Q = \frac{1}{R_{sys}} \sqrt{\frac{L_{sys}}{C_f}}, \text{ therefore, } H_{max} = Q.$$

Similar procedures are relied on to plot  $H_{fs}(j\omega)$  as shown in Fig. 9.6b.

### 9.3.2.2 First-Order Damped High-Pass Filter

Figure 9.7a shows the configuration of a first-order damped high-pass filter. A series connected resistance ( $R_f$ ) is included to provide a damping characteristic.

Filter transfer functions are

$$H_f(s) = Z_f(s) = \frac{V_f(s)}{I_f(s)} = R_f + \frac{1}{sC_f} \quad (9-6a)$$

$$H_{f_{sys}}(s) = Z_{f_{sys}}(s) = \frac{1}{\frac{1}{R_f + 1/sC_f} + \frac{1}{sL_{sys}}} \quad (9-6b)$$

$$H_{cds}(s) = H_{cds}(j\omega) = \frac{R_f + \frac{1}{j\omega C_f}}{R_f + \frac{1}{j\omega C_f} + j\omega L_{sys}} \quad (9-6c)$$

As discussed in the previous section,  $H_{cds}(s)$  can be determined analytically (Fig. 9.7c):

- For low frequencies ( $\omega \ll 1/\sqrt{L_{sys}C_f} \Rightarrow |1/j\omega C_f| \gg |j\omega L_{sys}|$ ):

$$H_{cds}(j\omega) \approx \frac{1}{j\omega C_f} = 1.$$

- For moderate high frequencies ( $1/\sqrt{L_{sys}C_f} < \omega < 1/R_f C_f \Rightarrow |1/j\omega C_f| \ll |j\omega L_{sys}|$ ):

$$H_{cds}(j\omega) \approx \frac{1}{j\omega L_{sys}} = \frac{-1}{\omega^2 L_{sys} C_f} \Rightarrow \text{roll-off is } 1/\omega^2 \text{ or } -40 \text{ dB per decade.}$$

- For high frequencies ( $\omega \gg 1/R_f C_f \Rightarrow R_f \gg |1/j\omega C_f|$  and  $|j\omega L_{sys}| \gg |R_f + 1/j\omega C_f|$ ):

$$H_{cds}(j\omega) = \frac{R_f + \frac{1}{j\omega C_f}}{j\omega L_{sys} + \left(R_f + \frac{1}{j\omega C_f}\right)} \approx \frac{R_f}{j\omega L_{sys}} \Rightarrow \text{roll-off is } 1/\omega \text{ or } -20 \text{ dB per decade.}$$

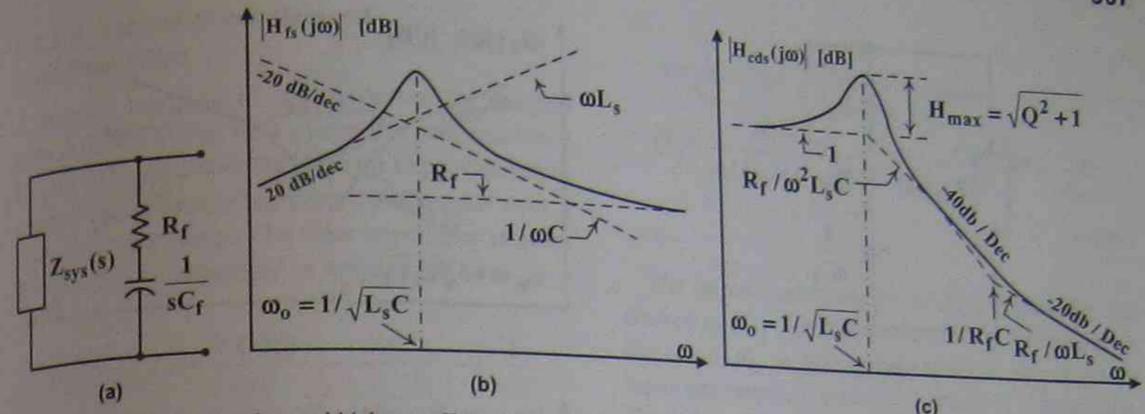


FIGURE 9.7 First-order damped high-pass filter; (a) equivalent circuit, (b) filter impedance transfer function, (c) current-divider transfer function.

- If the system resistance is included ( $Z_{sys}(s) = R_{sys} + sL_{sys}$ ), the maximum can be found as

$$H_{cds}(s = j\omega) \Big|_{\omega = \frac{1}{\sqrt{L_{sys}C_f}}} = 1 - j \frac{1}{R_{sys}} \sqrt{\frac{L_{sys}}{C_f}}$$

and

$$H_{max} = |H_{cds}(s = j\omega) \Big|_{\omega = \frac{1}{\sqrt{L_{sys}C_f}}} = \sqrt{Q^2 + 1} = Q$$

with  $Q = \frac{1}{R_{sys}} \sqrt{\frac{L_{sys}}{C_f}}$ .

Similar procedures are employed to plot  $H_{fs}(j\omega)$  as illustrated in Fig. 9.7b. Comparison of Figs. 9.6 and 9.7 indicates the following:

- the damping resistance significantly limits the high-frequency performance (e.g., roll-off of high-frequency components is only  $1/\omega$  or -20 dB per decade). Therefore, the damped filter is less desirable for telephone interference reduction applications; and
- for parallel resonant conditions (e.g., cancellation of  $L_{sys}$  by  $C_f$ ), if the resonant frequency falls on or near a critical harmonic frequency, a high-pass damping resistance ( $R_f$ ) can be used to control and reduce the amplification. However, this will increase the fundamental frequency power loss and reduces the effectiveness of the high-pass attenuation above the frequency  $1/(R_f C_f)$ .

### 9.3.2.3 Second-Order Band-Pass Filter

The second-order band-pass filter (also called single-tuned or series-resonant filter) is a series combination of capacitor ( $C_f$ ), inductor ( $L_f$ ), and a small damping resistor ( $R_f$ ), as depicted in Fig. 9.8a. The damping resistance is usually due to the internal resistance of either the inductor and/or capacitor. This filter is tuned to attenuate one single low-order harmonic. Typically, combinations of band-pass filters are used because the power system contains a number of dominant low-order harmonics.

Assuming a pure inductive system ( $Z_{sys}(s) = sL_{sys}$ ), filter transfer functions can be derived using Eqs. 9-1a and 9-2a:

$$H_f(s) = Z_f(s) = \frac{V_f(s)}{I_f(s)} = R_f + sL_f + \frac{1}{sC_f} = \frac{A}{s} \left[ 1 + \frac{1}{Q} \left( \frac{s}{\omega_0} \right) + \left( \frac{s}{\omega_0} \right)^2 \right] \quad (9-7)$$

$$H_{cds}(s) = H_{cds}(j\omega) = \frac{R_f + j\omega L_f + \frac{1}{j\omega C_f}}{R_f + j\omega L_f + \frac{1}{j\omega C_f} + j\omega L_{sys}} \quad (9-8)$$

where A is the gain. The filter quality factor (Q) and the series-resonant frequency ( $\omega_0$ ) are

$$Q = \frac{1}{R_f} \sqrt{\frac{L_f}{C_f}} \quad (9-9a)$$

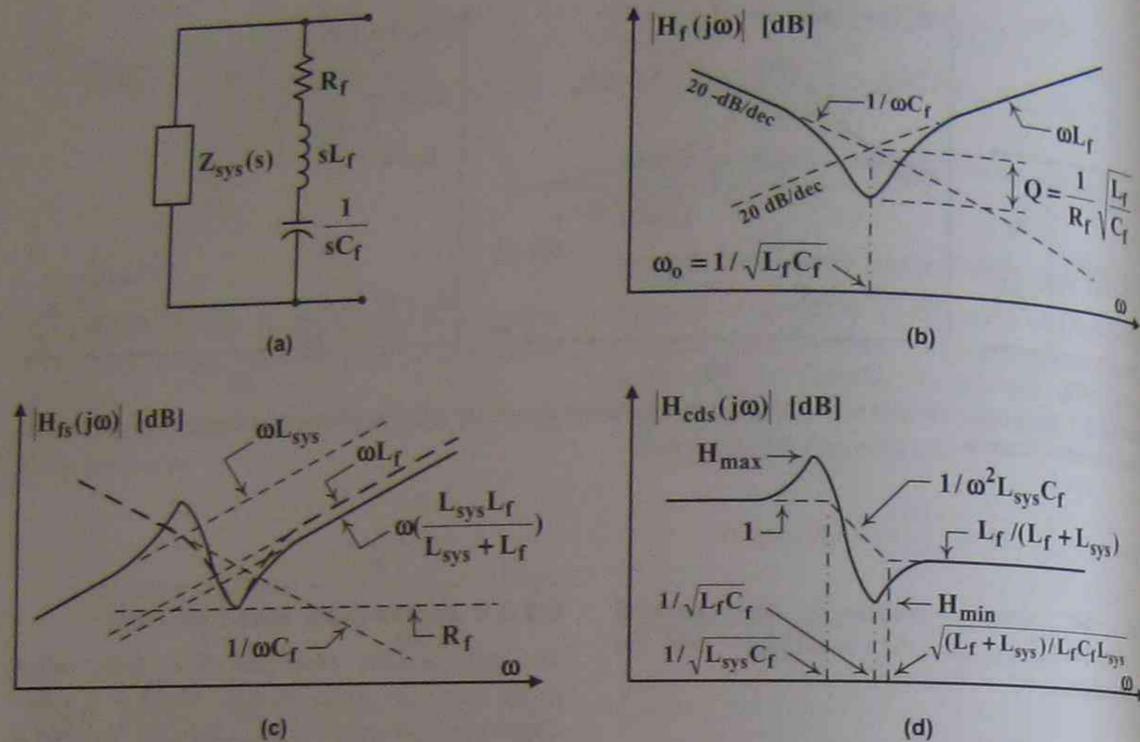


FIGURE 9.8 Second-order band-pass filter: (a) equivalent circuit, (b) filter impedance transfer function, (c) filter system impedance transfer function with  $L_{sys} > L_f$ , (d) current-divider transfer function with  $L_{sys} > L_f$ .

$$\omega_0 = \frac{1}{\sqrt{L_f C_f}} \quad (9-9b)$$

For high-voltage applications, the filter current has a low rms magnitude and does not require large current carrying conductors; therefore, air-core inductors are regularly used and the filter quality factor is relatively large (e.g.,  $50 < Q < 150$ ). For low-voltage applications, gapped iron-core inductors and conductors with a large cross section are employed (e.g.,  $10 < Q < 50$ ).

The filter impedance transfer function ( $H_f(j\omega)$ ) is presented graphically as shown in Fig. 9.8b. It is evaluated at low and high frequencies to determine its asymptotes:

- At low frequencies ( $\omega \ll \omega_0 \Rightarrow |1/j\omega C_f| \gg |R + j\omega L_{sys}|$ ), the filter is dominantly capacitive and provides reactive power to the system. Therefore,  $H_f(s) = 1/j\omega C_f$  and the roll-off of the low frequency components is  $-20$  dB per decade.
- At high frequencies ( $\omega \gg \omega_0 \Rightarrow |j\omega L_{sys}| \gg |R + 1/j\omega C_f|$ ), the filter is dominantly inductive and consumes reactive power with little influence on high-frequency distortions. Therefore,  $H_f(s) = j\omega L_f$  and the roll-off of the high frequency components is  $20$  dB per decade.

- At the resonant frequency ( $\omega = \omega_0$ ), the filter is entirely resistive, that is,  $H_f(s) = R_f$ . More attenuation is provided with lower filter resistances; however, there are practical limits to the value of  $R_f$ .

Similar procedures are applied to plot  $H_{fs}(j\omega)$  and  $H_{cds}(j\omega)$  as illustrated in Fig. 9.8c,d, respectively. Note that the minima of the transfer functions ( $H_{min}$ ) are very close to the series resonant frequency; however, due to the interaction between the capacitive reactance and the filter inductive reactance,  $H_{min}$  does not occur at the parallel resonant frequency formed by filter capacitance and system inductance. The derivatives of the transfer functions are usually evaluated numerically to determine frequencies where maxima occur.

The second-order band-pass (series resonant) filters are very popular and have many applications in power system design including transmission (e.g., connected in parallel at the AC terminals of HVDC converters), distribution (e.g., for detuning power factor capacitor banks to avoid parallel resonant frequencies), and utilization (e.g., across terminals of nonlinear loads).

### 9.3.2.4 Second-Order Damped Band-Pass Filter

A popular topology of the second-order damped filter is shown in Fig. 9.9a where a bypass resistance ( $R_{bp}$ ) is included across the inductor to provide attenuation for harmonic frequency components over a wide frequency range. The filter impedance transfer function can be expressed in normalized form

$$H_f(s) = \frac{V_f(s)}{I_f(s)} = \frac{1}{\frac{1}{R_{bp}} + \frac{1}{R_f + sL_f} + \frac{1}{sC_f}} = \frac{A}{s \left( 1 + \frac{s}{\omega_p} \right) \left[ 1 + \frac{1}{Q_{bp}} \left( \frac{s}{\omega_0} \right) + \left( \frac{s}{\omega_0} \right)^2 \right]}$$

(9-10a)

where the gain  $A$ , the series resonant angular frequency  $\omega_0$ , the quality factor  $Q_{bp}$ , and the pole frequency [13] for typical cases (whereby  $R_f \ll R_{bp}$ ) are

$$A = \frac{1}{C_f}, \quad \omega_0 = \sqrt{\frac{R_f + R_{bp}}{R_{bp} L_f C_f}} = \frac{1}{\sqrt{L_f C_f}},$$

$$Q_{bp} = \frac{R_f + R_{bp}}{\omega_0 (R_{bp} L_f C_f + L_f)}, \quad \omega_p = \frac{R_f + R_{bp}}{L_f} = \frac{R_{bp}}{L_f} \quad (9-10b)$$

The series resistance  $R_f$  is determined by the desired quality factor of the second-order band-pass filter and  $R_{bp}$  is selected to achieve the required high-pass response and series resonant attenuation. Typical values of the bypass quality factor are  $0.5 < Q_{bp} < 2.0$ . However, there is a trade-off between larger values (e.g., more series resonant attenuation and less high-pass response) and smaller values (e.g., less series resonant attenuation and greater high-pass response) of the quality factor.

### 9.3.2.5 Composite Filter

Higher order filters are constructed by increasing the number of storage elements (e.g., capacitors, inductors).

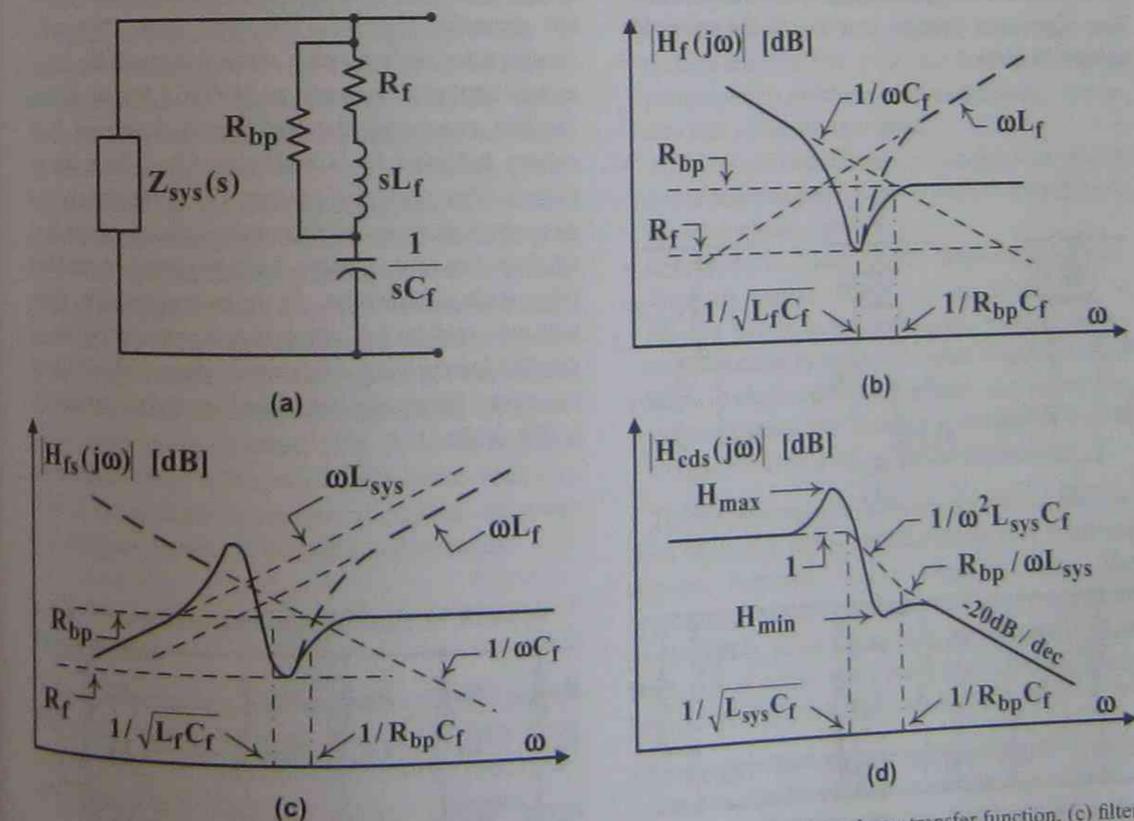


FIGURE 9.9 Second-order damped band-pass filter: (a) equivalent circuit, (b) filter impedance transfer function, (c) filter system impedance transfer function, (d) current-divider transfer function.

tors). However, their application in power systems is limited due to economic and reliability factors.

A third-order filter may be constructed by adding a series capacitance  $C_{f2}$  to the inductor bypass resistance (Fig. 9.10a) to limit  $I_{bp}$  and reduce the corresponding fundamental frequency losses or by including  $C_{f2}$  in series with  $L_f$  (Fig. 9.10b) and sizing it to form a series resonant branch at the fundamental frequency to reduce  $I_{bp}$  and to increase filter efficiency. If a second inductor  $L_{f2}$  is added to the circuit of Fig. 9.10a, a fourth-order double band-pass filter will be obtained, as shown in Fig. 9.10c.

A common type of an  $n$ th-order composite filter for power quality improvement is shown in Fig. 9.11. Several band-pass filters are connected in parallel and individually tuned to selected harmonic frequencies to provide compensation over a wide frequency range. The last branch is a high-pass filter attenuating high-order harmonics, which usually are a result of fast switching actions. Composite filters are only applied when even-order harmonics are small since a parallel resonance will occur between any two adjacent band-pass filter branches and cause amplification of the distortion in that frequency range. For example, composite filter systems with shunt branches tuned at the 5th and 7th harmonics will have a resonant frequency about at the 6th harmonic. The impedance transfer function of the  $n$ th-order composite filter is

$$H_f(s) = Z_f(s) = \frac{V_f(s)}{I_f(s)} = \frac{1}{\frac{1}{Z_f^{(3)}} + \frac{1}{Z_f^{(7)}} + \frac{1}{Z_f^{(11)}} + \dots + \frac{1}{Z_f^{(n)}}} \quad (9-11)$$

It is time-consuming to derive the transfer functions of multiple-order filters in terms of factorized expressions of poles and zeros [13]. Therefore, numerical approaches are typically applied to plot the transfer function, and an iterative design procedure is used to optimize a filter configuration.

### 9.3.3 Classification of Passive Power Filters

Passive filters cause harmonic currents to flow at their resonant frequency. Due to this resonance, the harmonic currents are attenuated in the power system through the LC filter circuits tuned to the harmonic orders that require filtering. In practice, a single passive filter is not adequate since there is more than one harmonic to be attenuated; therefore, a shunt or series passive composite filter unit (Fig. 9.12) is used. Passive filter units are generally designed to remove a few low-order harmonics, for example, the 5th, 7th, and 11th. Normally passive filter units employ three (or more for high-power applications such as HVDC) tuned filters, the first two being for the lowest dominant harmonics followed by a high-pass filter. In a shunt passive filter unit, two lossless LC components are connected in series to sink harmonic currents and all three (or more) filters are connected in parallel (Fig. 9.12a). However, in a series passive filter unit, two lossless LC components are connected in parallel for creating a harmonic dam and all three (or more) filters are connected in series, as shown in Fig. 9.12b.

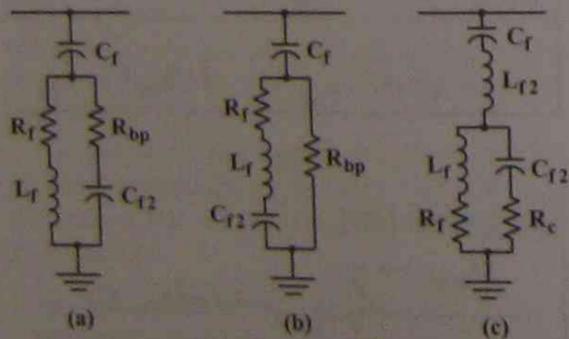


FIGURE 9.10 Higher order filters; (a) and (b) third-order filters, (c) fourth-order filter.

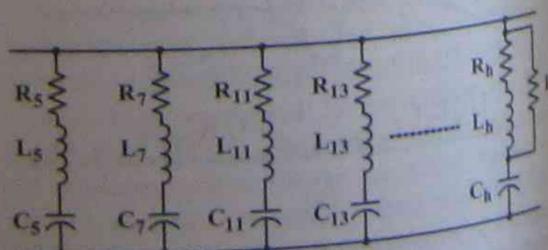


FIGURE 9.11 Nth-order composite filter.

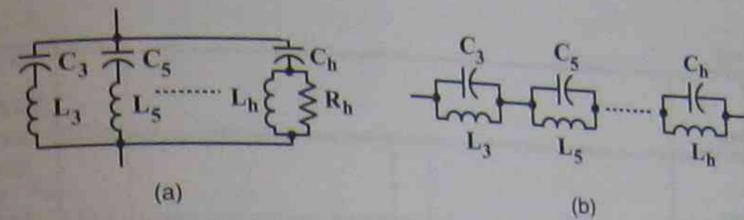


FIGURE 9.12 Typical passive filter unit employing a number of tuned filter units, the first  $(h-1)$  units are tuned to the lowest dominant harmonic frequencies followed by a high-pass element; (a) shunt passive filter block, (b) series passive filter block.

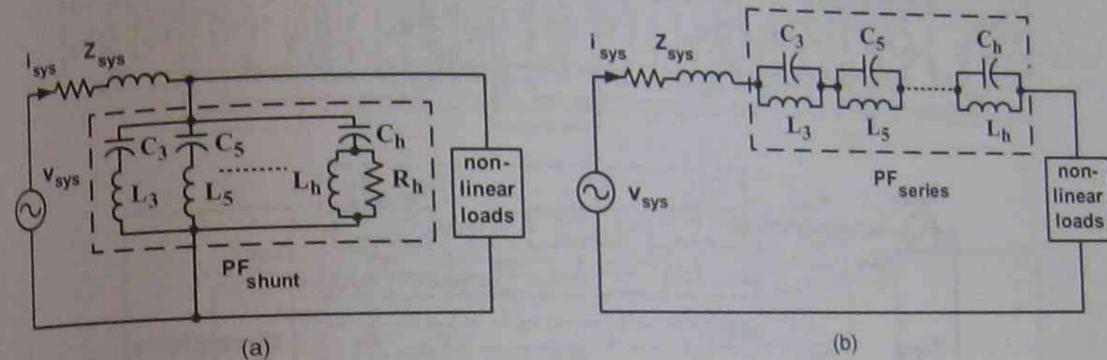


FIGURE 9.13 Single-phase passive filter; (a) shunt configuration, (b) series configuration.

The inductors should have high quality factors to reduce system losses and must not saturate in the entire current operating region. Capacitor values are decided by the required reactive power of the system, and then inductor values are calculated by tuning them for the particular harmonic frequencies. Resistor values are calculated by the corresponding quality factors based on the desired sharpness of the characteristics. Similarly, the resistance of the high-pass filter is computed based on the sharpness or attenuation of the higher order harmonics on the one hand, and reducing the losses on the other hand to achieve an optimum value for the quality factor. Passive filter units with shunt and series configurations are extensively used in single-phase (Fig. 9.13), three-phase three-wire (Fig. 9.14), and three-phase four-wire (Fig. 9.15) systems to improve the quality of power and mitigate harmonic currents and voltages.

### 9.3.4 Potentials and Limitations of Passive Power Filters

Design, construction, and implementation of passive filters are straightforward and easier than their counterparts, for example, synchronous condensers and active filters. They have many advantages:

- they are robust, economical, and relatively inexpensive;

- they can be implemented in large sizes of MVARs and require low maintenance;
- they can provide a fast response time (e.g., one cycle or less with SVC), which is essential for some power quality problems such as flickering voltage dips due to arc-furnace loads;
- unlike rotating machines (e.g., synchronous motors or condensers) passive filters do not contribute to the short-circuit currents; and
- in addition to power quality improvement, well-designed passive filters can be configured to provide power factor correction, reactive power compensation, or voltage support (e.g., on critical buses in case of a source outage) and reduce the starting impact and associated voltage drops due to large loads (e.g., large induction motors).

These advantages have resulted in broad applications of passive filters in different sectors of power systems. However, power engineers have also encountered some limitations and shortcomings of passive filters, which have called for alternative solutions such as active and hybrid filter systems. Some limitations of passive filters are as follows:

- fixed compensation or harmonic mitigation, large size, and possible resonance with the supply system impedance at fundamental and/or other harmonic frequencies;

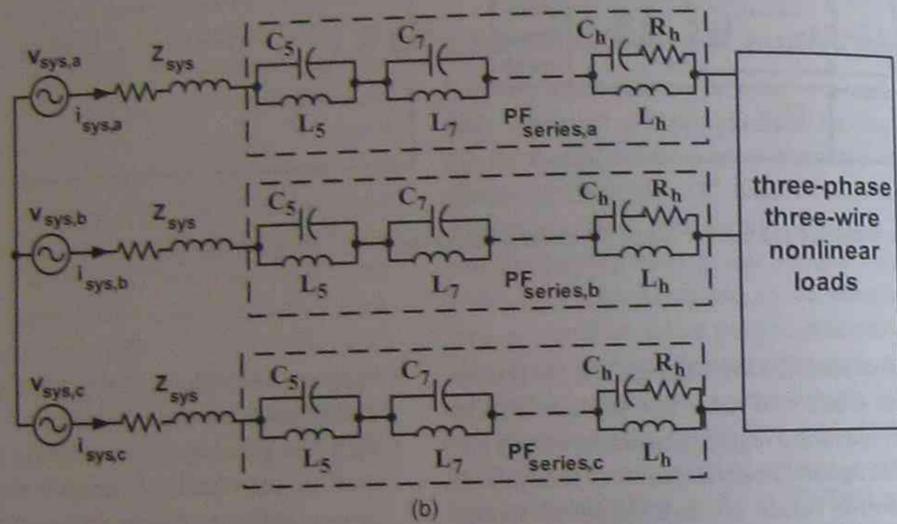
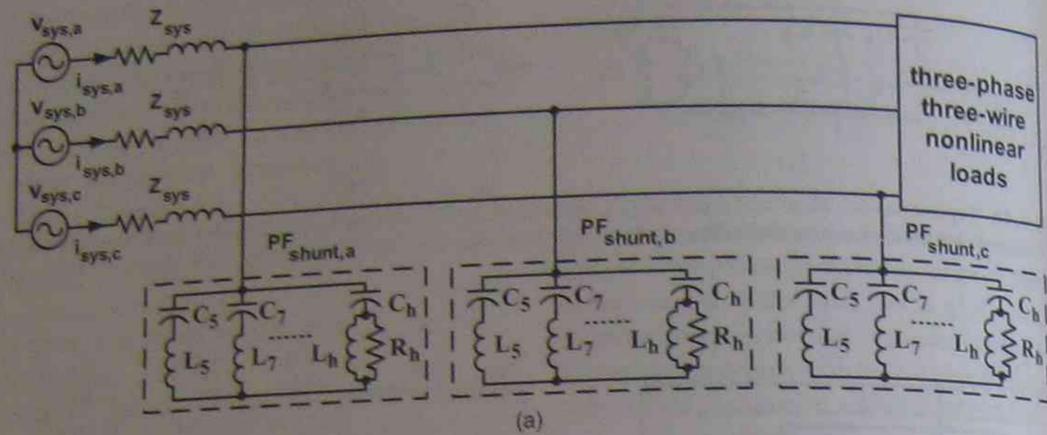


FIGURE 9.14 Three-phase three-wire passive filter; (a) shunt configuration, (b) series configuration [4].

- compensation is limited to a few orders of harmonics;
- once installed, the tuned frequency and/or filter size cannot be changed easily;
- unsatisfactory performance (e.g., detuning) may occur due to variations of filter parameters (caused by aging, deterioration, and temperature effects) and nonlinear load characteristics;
- change in system operating conditions (e.g., inclusion of capacitors and/or other filters) has large influence on filter designs. Therefore, to be effective, filter impedance should be less than system impedance, which can become a problem for strong or stiff systems [2];
- resonance between system and filter (e.g., shifted resonance frequency) for single- and double-

- tuned filters can cause an amplification of characteristics and noncharacteristic harmonic currents. Therefore, the designer has a limited choice in selecting tuned frequencies and ensuring adequate bandwidth between shifted frequencies and integer (even and odd) harmonics [2];
- special protective and monitoring devices might be required to control switching surges, although filter reactors will reduce the magnitude of the switching inrush current magnitude and its associated high frequency; and
- stepless control (of reactive power, power factor correction, and voltage support) is not possible since the filter can either be switched on or switched off only.

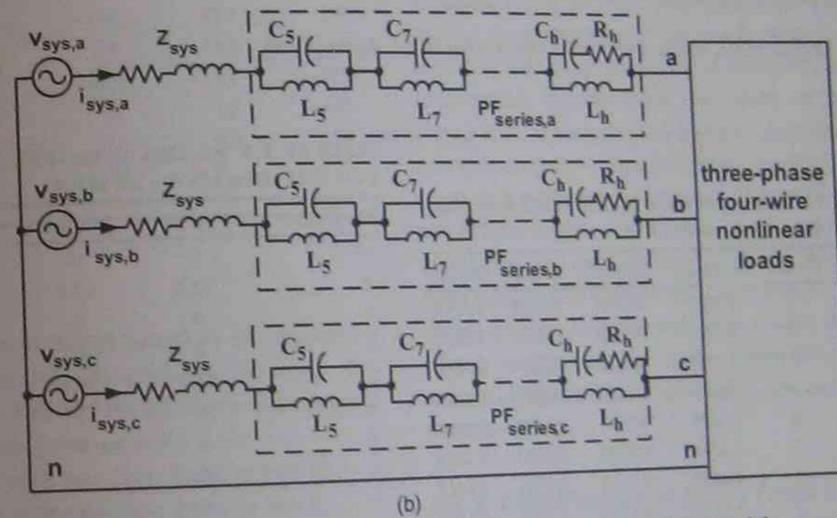
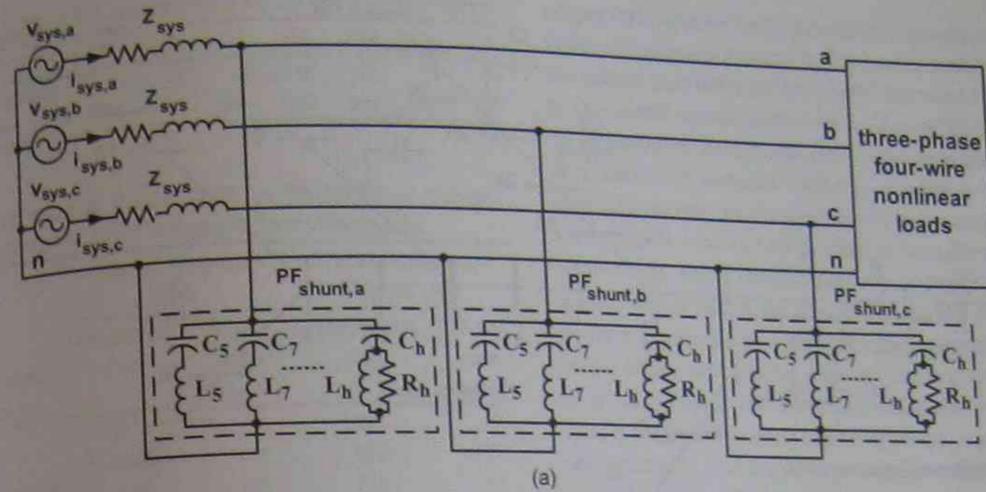


FIGURE 9.15 Three-phase four-wire passive filter; (a) shunt configuration, (b) series configuration [4].

**9.3.5 Application Example 9.1: Hybrid Passive Filter Design to Improve the Power Quality of the IEEE 30-Bus Distribution System Serving Adjustable-Speed Drives**

Consider the IEEE 23 kV, 30-bus distribution system [9, 10] shown in Fig. E9.1.1. System transmission-line data, bus data, and capacitor data are provided in Tables E9.1.1 to E9.1.3, respectively. To investigate the impact of large AC drive systems on the power quality of the distribution system, a PWM adjustable-speed drive (675 kW, 439 kVAr) and a variable-frequency drive (350 kW, 175 kVAr) are connected to buses 15 and 18, respectively. Table E9.1.4 depicts the spectra of the current harmonics

injected by typical AC drives into the system. Use harmonic current sources to model the two nonlinear loads and utilize the decoupled harmonic power flow algorithm (Chapter 7, Section 7.5.1) to simulate the system. Determine the total harmonic voltage distortion (THD<sub>v</sub>) of the system and at the individual buses before and after the installation of the hybrid passive filter banks listed below. Plot the voltage and current waveforms at bus 15 before and after filtering.

- a) Two filter banks are placed at the terminals of nonlinear loads (buses 15 and 18). Each bank consists of a number of shunt-connected series

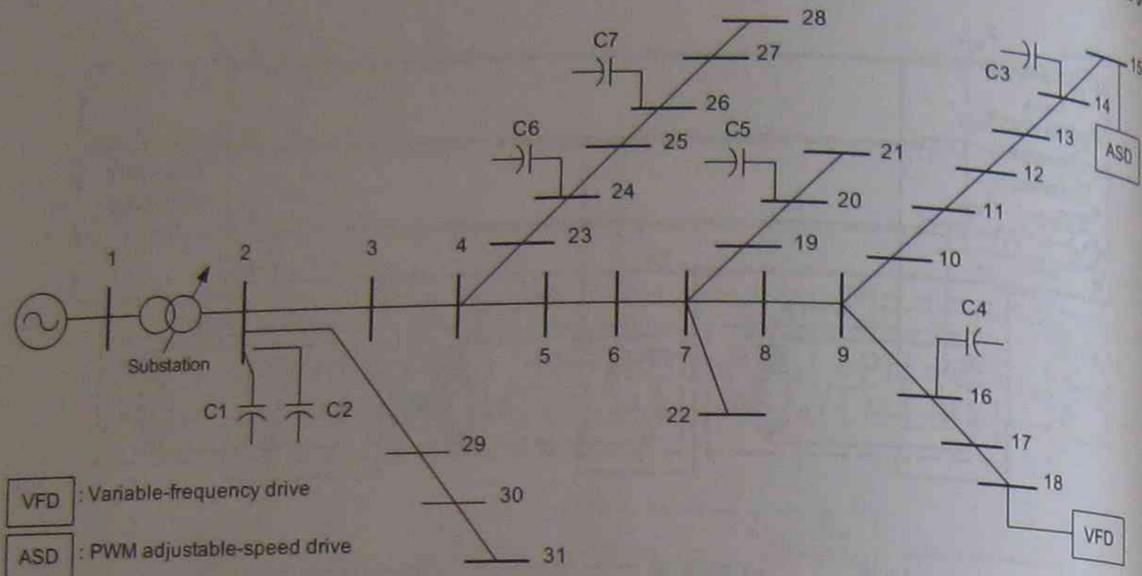


FIGURE E9.1.1 IEEE 30-bus system with two nonlinear AC drives [9, 10].

TABLE E9.1.1 Line Data for the IEEE 30-Bus System (Base kV = 23 kV, Base MVA = 100 MVA)

From bus	To bus	R (ohm)	X (ohm)	R (pu)	X (pu)
1	2	0.0021	0.0365	0.0004	0.0069
2	3	0.2788	0.0148	0.0527	0.0028
3	4	0.4438	0.4391	0.0839	0.0830
4	5	0.8639	0.7512	0.1633	0.1420
5	6	0.8639	0.7512	0.1633	0.1420
6	7	1.3738	0.7739	0.2597	0.1463
7	8	1.3738	0.7739	0.2597	0.1463
8	9	1.3738	0.7739	0.2597	0.1463
9	10	1.3738	0.7739	0.2597	0.1463
10	11	1.3738	0.7739	0.2597	0.1463
11	12	1.3738	0.7739	0.2597	0.1463
12	13	1.3738	0.7739	0.2597	0.1463
13	14	1.3738	0.7739	0.2597	0.1463
14	15	1.3738	0.7739	0.2597	0.1463
9	16	0.8639	0.7512	0.1633	0.1420
16	17	1.3738	0.7739	0.2597	0.1463
17	18	1.3738	0.7739	0.2597	0.1463
7	19	0.8639	0.7512	0.1633	0.1420
19	20	0.8639	0.7512	0.1633	0.1420
20	21	1.3738	0.7739	0.2597	0.1463
7	22	0.8639	0.7512	0.1633	0.1420
4	23	0.4438	0.4391	0.0839	0.0830
23	24	0.4438	0.4391	0.0839	0.0830
24	25	0.8639	0.7512	0.1633	0.1420
25	26	0.8639	0.7512	0.1633	0.1420
26	27	0.8639	0.7512	0.1633	0.1420
27	28	1.3738	0.7739	0.2597	0.1463
2	29	0.2788	0.0148	0.0527	0.0028
29	30	0.2788	0.0148	0.0527	0.0028
30	31	1.3738	0.7739	0.2597	0.1463

TABLE E9.1.2 Bus Data for the IEEE 30-Bus System (Base kV = 23 kV, Base MVA = 100 MVA)

Bus number	P (kW)	Q (kVAr)	P (pu)	Q (pu)
1*	0	0	0	0
2	52.2	17.2	0.522	0.172
3	0	0	0	0
4	0	0	0	0
5	93.8	30.8	0.938	0.308
6	0	0	0	0
7	0	0	0	0
8	0	0	0	0
9	0	0	0	0
10	18.9	6.2	0.189	0.062
11	0	0	0	0
12	33.6	11	0.336	0.11
13	65.8	21.6	0.658	0.216
14	78.4	25.8	0.784	0.258
15	73	24	0.73	0.24
16	47.8	15.7	0.478	0.157
17	55	18.1	0.55	0.181
18	47.8	15.7	0.478	0.157
19	43.2	14.2	0.432	0.142
20	67.3	22.1	0.673	0.221
21	49.6	16.3	0.496	0.163
22	20.7	6.8	0.207	0.068
23	52.2	17.2	0.522	0.172
24	192	63.1	1.92	0.631
25	0	0	0	0
26	111.7	36.7	1.117	0.367
27	55	18.1	0.55	0.181
28	79.3	26.1	0.793	0.261
29	88.3	29	0.883	0.29
30	0	0	0	0
31	88.4	29	0.884	0.29

\*Swing bus.

TABLE E9.1.3 Capacitor Data for the IEEE 30-Bus System

Capacitor	C1	C2	C3	C4	C5	C6	C7
Bus location	2	2	14	16	20	24	26
kVAr	900	600	600	600	300	900	900

TABLE E9.1.4 Typical Harmonic Spectrum of Variable-Frequency and PWM Adjustable-Speed Drives [14]

Harmonic order h	Variable-frequency drive		PWM adjustable-speed drive	
	Magnitude (%)	Phase angle (degree)	Magnitude (%)	Phase angle (degree)
1	100	0	100	0
5	23.52	111	82.8	-135
7	6.08	109	77.5	69
11	4.57	-158	46.3	-62
13	4.2	-178	41.2	139
17	1.8	-94	14.2	9
19	1.37	-92	9.7	-155
23	0.75	-70	1.5	-158
25	0.56	-70	2.5	98
29	0.49	-20	0	0
31	0.54	7	0	0

resonance passive filters tuned at the respective dominant harmonic frequencies. Assume  $R_f = 100 \Omega$  and  $L_f = 100 \text{ mH}$  for all filters and compute the corresponding values of  $C_f$ .

- b) Repeat part a with one filter bank at bus 15.
- c) Repeat part b with one filter bank at bus 9.
- d) Compare the results of parts a to c and make comments regarding the impact of numbers and locations of filters on the power quality of the system.

9.4 ACTIVE FILTERS

Active filters (AFs) are feasible alternatives to passive filters (PFs). For applications where the system configuration and/or the harmonic spectra of nonlinear loads (e.g., orders, magnitudes, and phase angles) change, active elements may be used instead of the passive components to provide dynamic compensation.

An active filter is implemented when the order numbers of harmonic currents are varying. This may be due to the nature of nonlinear loads injecting time-dependent harmonic spectra (e.g., variable-speed drives) or may be caused by a change in the system configuration. The structure of an active filter may be that of series or parallel architectures. The

proper structure for implementation depends on the types of harmonic sources in the power system and the effects that different filter solutions would cause to the overall system performance. Active filters rely on active power conditioning to compensate undesirable harmonic currents replacing a portion of the distorted current wave stemming from the nonlinear load. This is achieved by producing harmonic components of equal amplitude but opposite phase angles, which cancel the injected harmonic components of the nonlinear loads. The main advantage of active filters over passive ones is their fine response to changing loads and harmonic variations. In addition, a single active filter can compensate more than one harmonic, and improve or mitigate other power quality problems such as flicker.

Active filters are expensive compared with their passive counterparts and are not feasible for small facilities. The main drawback of active filters is that their rating is sometimes very close to the load (up to 80% in some typical applications), and thus it becomes a costly option for power quality improvement in a number of situations. Moreover, a single active filter might not provide a complete solution in many practical applications due to the presence of both voltage and current quality problems. For such cases, a more complicated filter design consisting of two or three passive and/or active filters (called a hybrid filter) is recommended as discussed in Section 9.5.

9.4.1 Classification of Active Power Filters Based on Topology and Supply System

Active filters have become a mature technology for harmonic and reactive power compensation of single- and three-phase electric AC power networks with high penetration of nonlinear loads. This section classifies active filters based on the supply system taking into consideration their (shunt or/and series) topology. Therefore, there are six types of shunt and series connected active filters for single-phase two-wire, three-phase three-wire, and three-phase four-wire AC networks, as shown in Figs. 9.16, 9.17, and 9.18, respectively. Composite filters consisting of two or more active filters are realized as hybrid filters and are discussed in Section 9.5.

9.4.2 Classification of Active Power Filters Based on Power Rating

Active filters can also be classified according to their power rating and speed of response required for their application in a compensated system [5]:

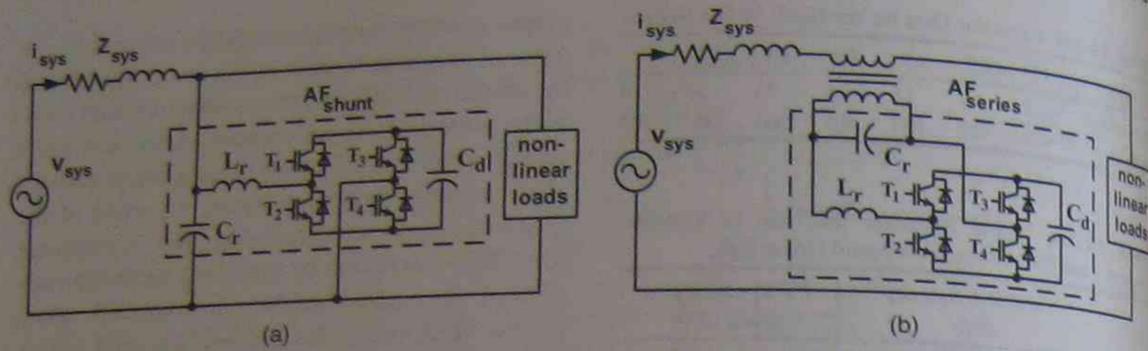


FIGURE 9.16 Single-phase active filter (AF): (a) shunt configuration, (b) series configuration [4].

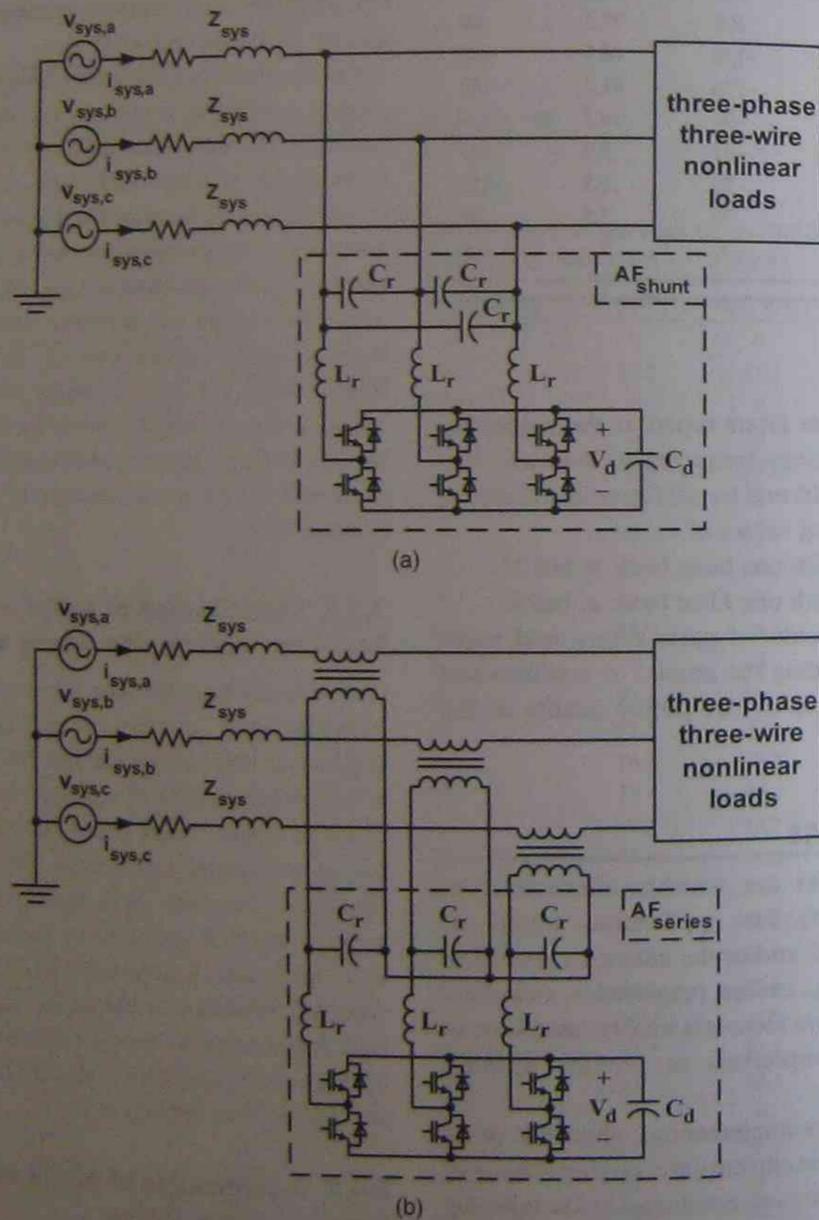


FIGURE 9.17 Three-phase three-wire active filter: (a) shunt configuration, (b) series configuration.

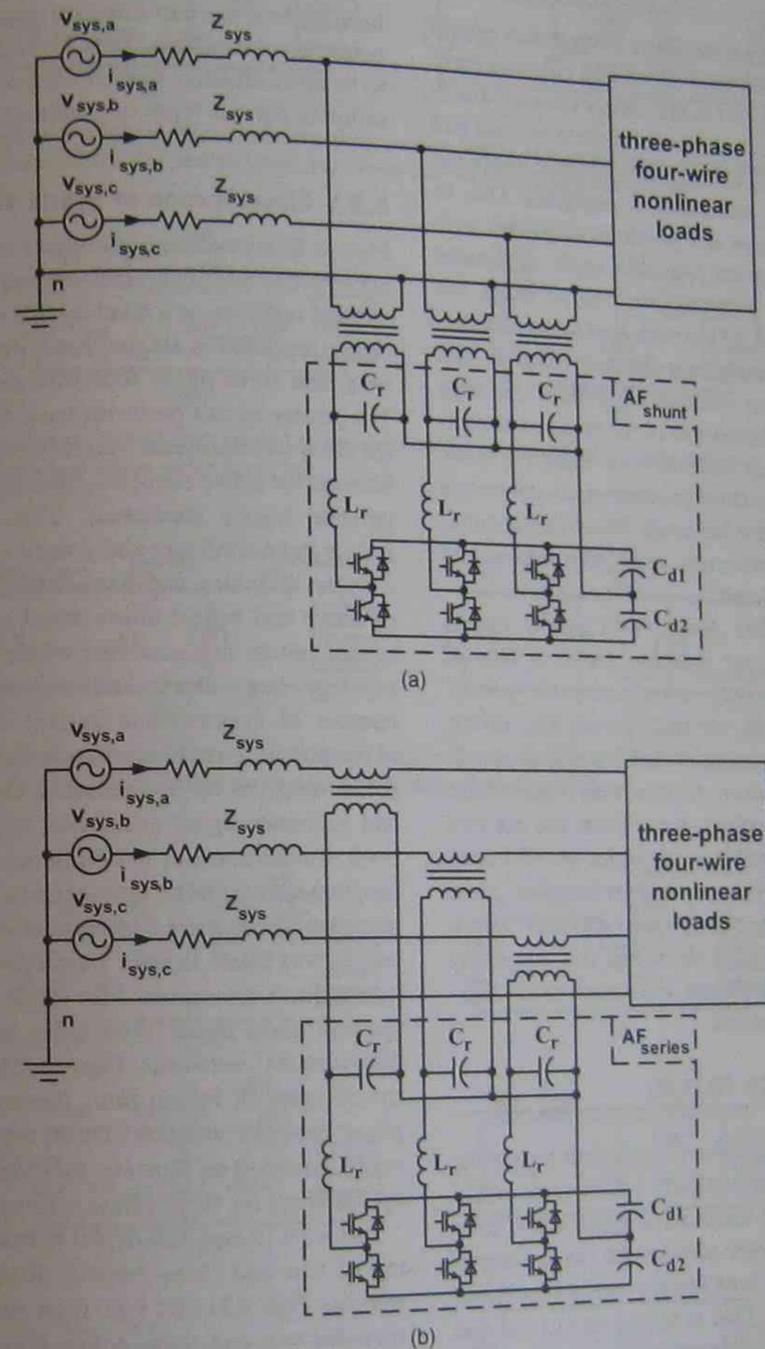


FIGURE 9.18 Three-phase four-wire active filter: (a) shunt configuration, (b) series configuration [4].

- **Low-power active filters** (with power ratings below 100 kVA and response times of about 10  $\mu$ s to 10 ms) are mainly used in residential areas, small to medium-sized factories, electric drives, commercial buildings, and hospitals. These applications require sophisticated dynamic filtering techniques and include single-phase and three-phase systems.
- Single-phase active filters are mainly available for low power ratings, and hence can be operated at

relatively high frequencies leading to improved performance and lower prices. They have many retrofit applications such as commercial and educational buildings with many computer loads.

- For balanced three-phase low power applications a three-phase filter can be used. However, for unbalanced load currents or unsymmetrical supply voltages, especially in three-phase four-wire distribution systems, three single-phase filters or a hybrid filter are usually required.

• **Medium-power active filters** (with power ratings of about 100 kVA to 10 MVA and response times of about 100 ms to 1 s) are mainly associated with medium- to high-voltage distribution systems and high-power, high-voltage drive systems, where the effect of phase imbalance is negligible. Due to economic concerns and problems associated with high-voltage systems (isolation, series or parallel connections of switches, etc.), these filters are usually designed to perform harmonic cancellation, and reactive-power compensation is not included in their control algorithms. At high voltage, other approaches of reactive power compensation such as capacitive or inductive static compensators, synchronous condensers, controlled LC filters, tuneable harmonic filters, line-commutated thyristor converters, and VAR compensators should be considered.

• **High-power active filters** (with power ratings above 10 MVA and response times of tens of seconds) are mainly associated with power-transmission grids, ultrahigh-power DC drives, and HVDC. Due to the availability of high switching-frequency power devices with high-voltage and high-power ratings, these filters are not cost effective. It is possible to use series-parallel combinations of low-power switches; however, there are many implementation issues and cost considerations. Fortunately, there are not too many power quality problems associated with high-voltage power systems.

9.5 HYBRID POWER FILTERS

A major drawback of active filters is their high rating (e.g., up to 80% of the nonlinear load in some practical applications). In addition, a single active filter cannot offer a complete solution for the simultaneous compensation of both voltage and current power quality disturbances. Due to higher ratings and cost considerations, the acceptability of active filters has been limited in practical applications. In response to these factors, different structures of hybrid filters

have evolved as a cost-effective solution for the compensation of nonlinear loads. Hybrid filters are found to be more effective in providing complete compensation of various types of nonlinear loads.

9.5.1 Classification of Hybrid Filters

Hybrid filters combine a number of passive and/or active filters and their structure may be of series or parallel topology or a combination of the two. They can be installed in single-phase, three-phase three-wire, and three-phase four-wire distorted systems. The passive circuit performs basic filtering action at the dominant harmonic frequencies (e.g., 5th or 7th) whereas the active elements, through precise control, mitigate higher harmonics. This will effectively reduce the overall size and cost of active filtering.

In the literature, there are different classifications of active and hybrid filters based on power rating, supply system (e.g., number of wires and phases), topology (e.g., shunt and/or series connection), number of (passive and active) elements, speed of response, power circuit configuration, system parameter(s) to be compensated, control approach, and reference-signal estimation technique. In this book, classification of hybrid filters is based on the supply system with the topology as a further subclassification. If there are a maximum of three (passive and active) filters in each phase, then 156 types of hybrid filters are expected for single-phase two-wire systems, three-phase three-wire, and three-phase four-wire AC networks. Figures 9.19 to 9.25 show the 52 types of hybrid filter topologies for single-phase two-wire systems. These topologies can be easily extended to illustrate the other 104 types of hybrid filters for three-phase systems.

Figures 9.19 and 9.20 depict hybrid filters consisting of two and three passive filters, respectively, whereas Figs. 9.21 and 9.22 show similar configurations for two and three active filters. There are 8 topologies of hybrid filters consisting of one passive and one active filter as shown in Fig. 9.23. There are many possible combinations if three filters are

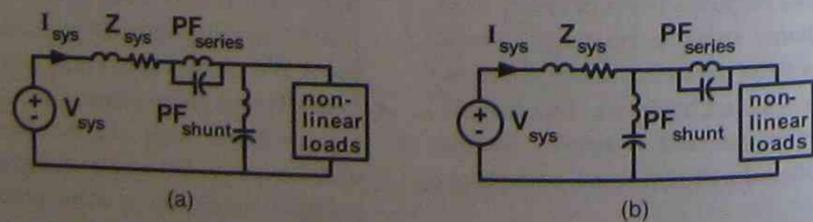


FIGURE 9.19 Single-phase hybrid filter (including two passive filters) as a combination of (a) passive-series and passive-shunt filters, (b) passive-shunt and passive-series filters [4].

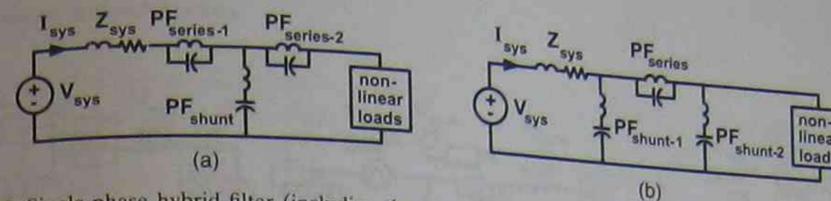


FIGURE 9.20 Single-phase hybrid filter (including three passive filters) as a combination of (a) passive-series, passive-series, and passive-shunt filters, (b) passive-shunt, passive-series, and passive-shunt filters [4].

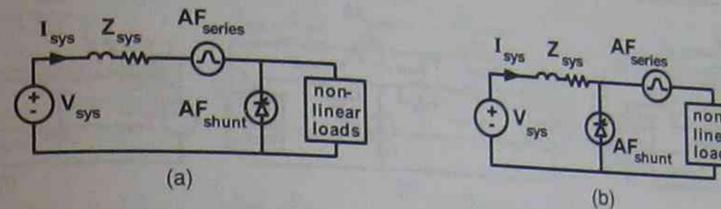


FIGURE 9.21 Single-phase hybrid filter (including two active filters) as a combination of (a) active-series and active-shunt filters, (b) active-shunt and active-series filters [4].

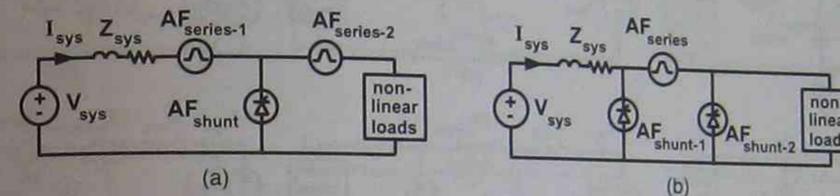


FIGURE 9.22 Single-phase hybrid filter (including three active filters) as a combination of (a) active-series, active-series, and active-shunt filters, (b) active-shunt, active-series, and active-shunt filters [4].

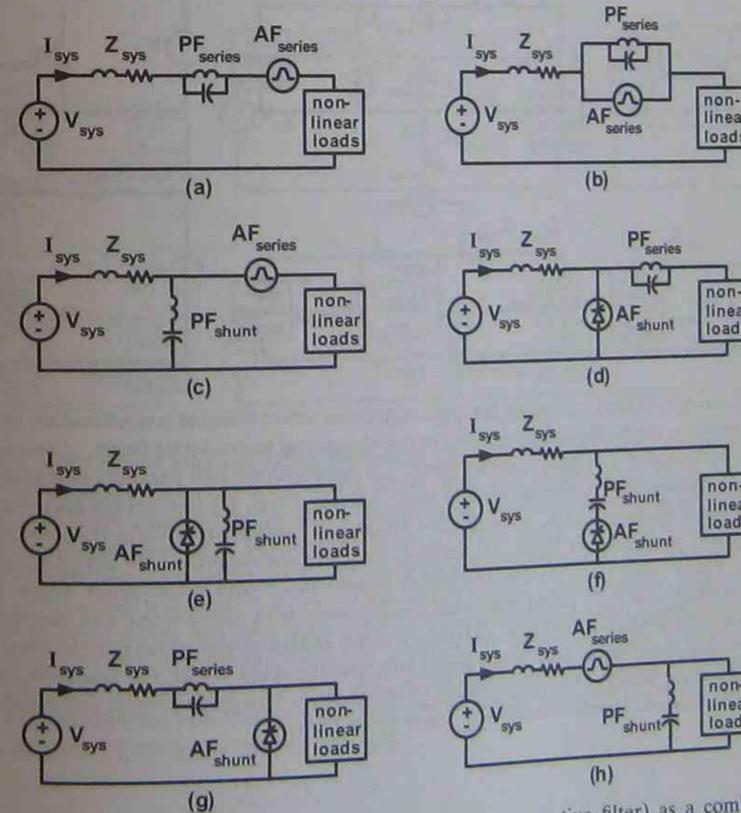
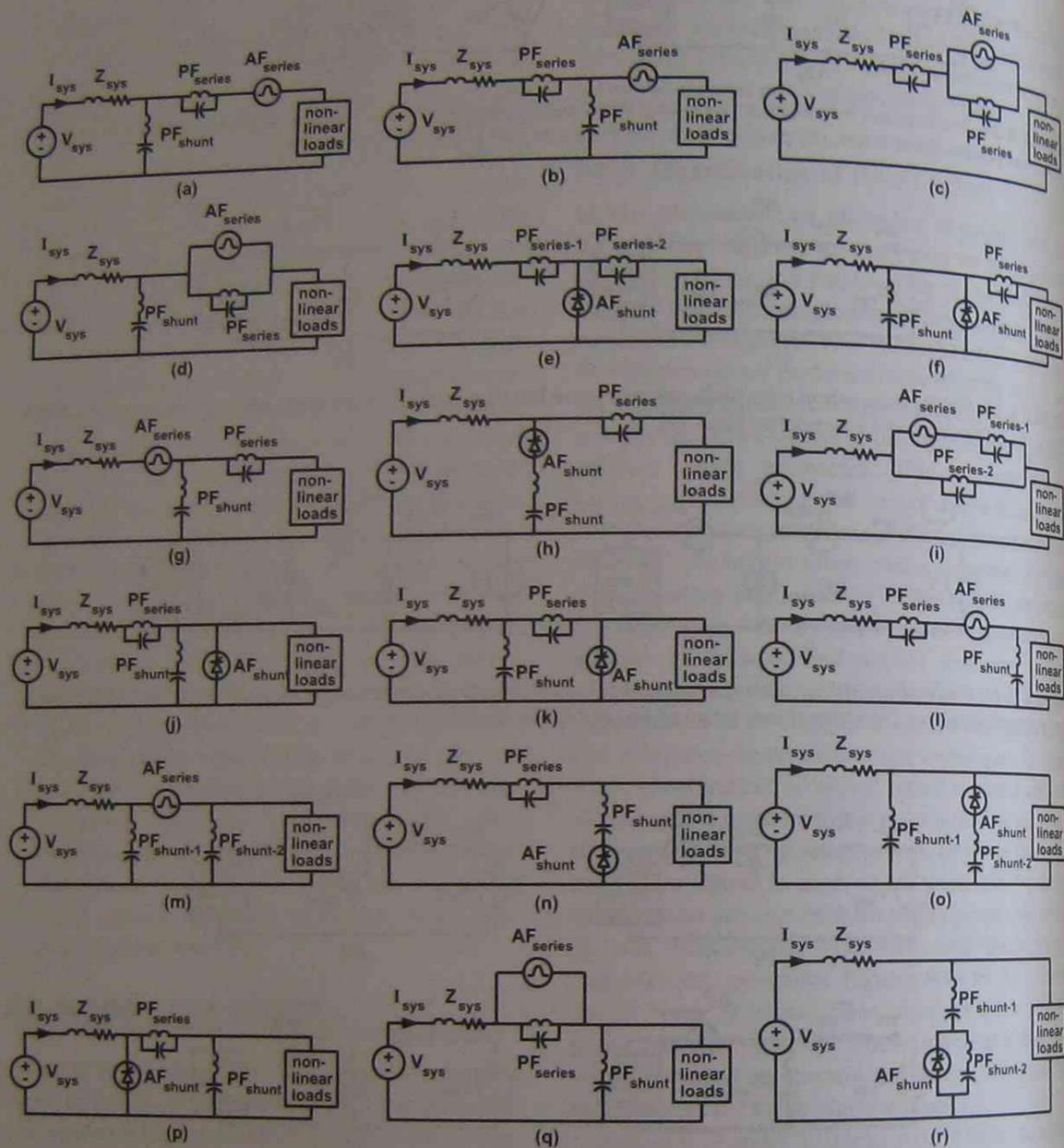
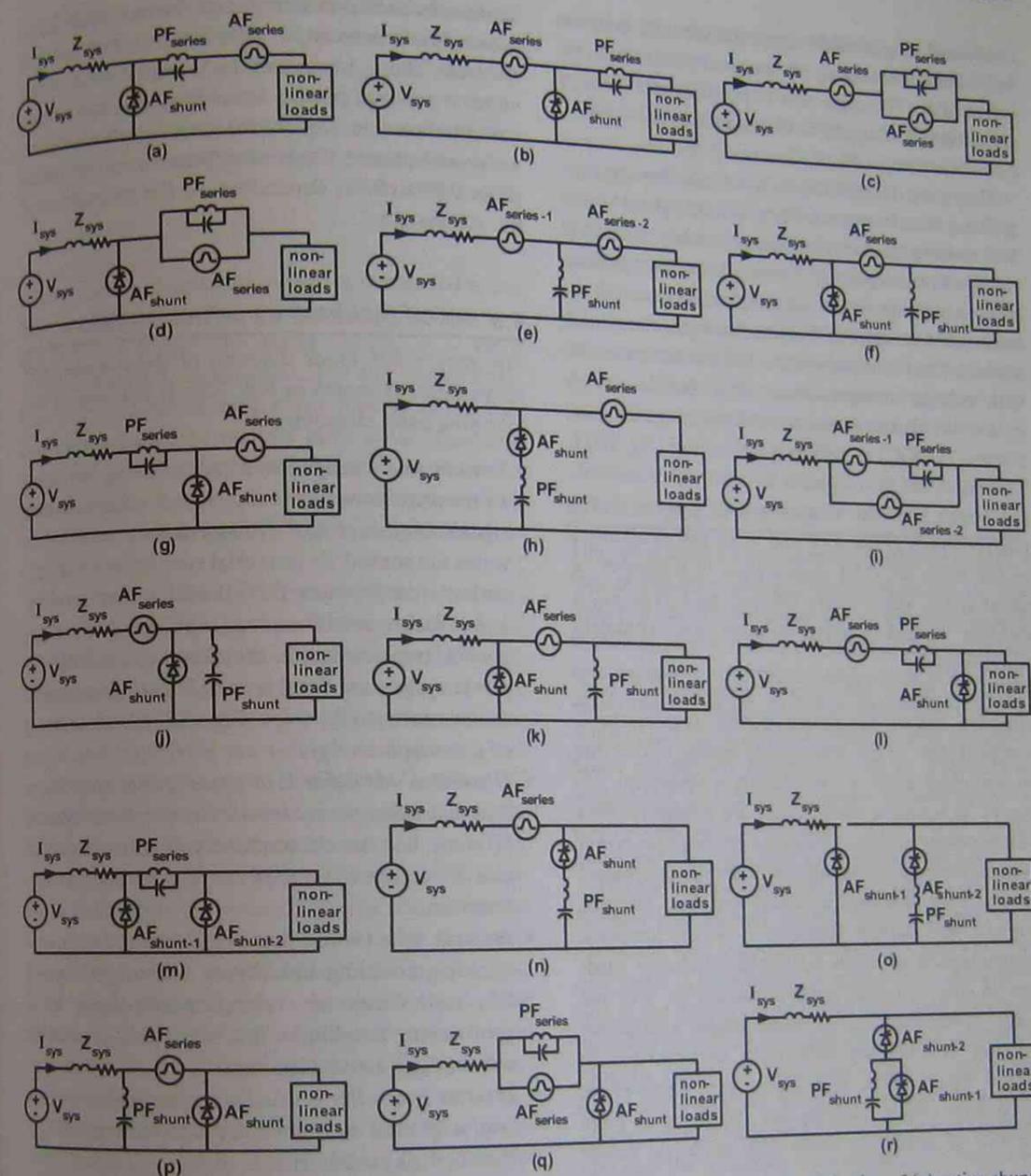


FIGURE 9.23 Single-phase hybrid filter (including one passive and one active filter) as a combination of (a) series-connected passive-series and active-series filters, (b) parallel-connected passive-series and active-series filters, (c) passive-shunt and active-series filters, (d) active-shunt and passive-series filters, (e) active-shunt and passive-shunt filters, (f) series-connected passive-shunt and active-shunt filters, (g) passive-series and active-shunt filters, (h) active-series and passive-shunt filters [4].

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**FIGURE 9.24** Single-phase hybrid filter (including two passive and one active filter) as a combination of (a) passive-shunt, passive-series, and active-series filters, (b) passive-series, passive shunt, and active-series filters, (c) passive-series in series with parallel-connected active-series and passive-series filters, (d) passive-shunt and parallel-connected active-series and passive-series filters, (e) passive-series, active-shunt, and passive-series filters, (f) parallel-connected passive-shunt with active-shunt and passive-series filters, (g) active-series, passive-shunt, and passive-series filters, (h) series-connected passive-shunt with active-series and passive-series filters, (i) series-connected passive-series with active-series in parallel with passive-series filters, (j) passive-series and parallel-connected passive-shunt with active-shunt filters, (k) passive-shunt, passive-series, and active-shunt filters, (l) series-connected passive-series with active-series and passive-shunt filters, (m) passive-shunt, active-series, and passive-shunt filters, (n) passive-series and series-connected passive-shunt with active-shunt filters, (o) passive-shunt and series-connected active-series with passive-shunt filters, (p) combination of active-shunt, passive-series, and passive-shunt filters, (q) parallel-connected active-series with passive-series and passive-shunt filters, (r) passive-shunt and parallel-connected passive-shunt with active-series filters [4].



**FIGURE 9.25** Single-phase hybrid filter (including one passive and two active filters) as a combination of (a) active-shunt, active-series, and passive-series filters, (b) active-series, active-shunt, and passive-series filters, (c) active-series, parallel-connected passive-series with active-series filters, (d) active-shunt, parallel-connected passive-series with active-series filters, (e) active-series, passive-shunt, and active-series filters, (f) active-shunt, passive-shunt, and active-series filters, (g) active-series, active-shunt, and active-series filters, (h) series-connected active-shunt with passive-shunt and active-series filters, (i) active-series in parallel with passive-series and active-series filters, (j) active-series, active-shunt and passive-shunt filters, (k) active-shunt, active-series, and passive-shunt filters, (l) active-series, passive-series, and active-shunt filters, (m) active-shunt, passive-series, and active-shunt filters, (n) active-series, series-connected active-shunt, and passive-shunt filters, (o) active-shunt, series-connected active-shunt, and passive-shunt filters, (p) passive-shunt, active-series, and active-shunt filters, (q) parallel-connected passive-series with active-series and active-shunt filters, (r) active-shunt in series with parallel-connected active-shunt and passive-shunt filters [4].

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combined. Figure 9.24 illustrates the 18 possible hybrid filters consisting of two passive filters and one active filter. There are also 18 possible hybrid filters consisting of one passive filter and two active filters as represented in Fig. 9.25.

The rating of active filters is reduced through augmenting them by passive filters to form hybrid filters. This reduces the overall cost and in many cases provides better compensation than when either passive or active filters alone are employed. However, a more efficient approach is to combine shunt and series active filters, which can provide both current and voltage compensation. This (active-active) hybrid filter is known as a unified power quality conditioner (UPQC) or universal active filter (Fig. 9.21). Therefore, the development in hybrid filter technology began from the arrangement of (two or three) passive filters (Figs. 9.19 and 9.20) and progressed to the more effective combination of a number of shunt and/or series active filters (Figs. 9.21 to 9.25), yielding a cost-effective solution and complete compensation.

Hybrid filters are usually considered a cost-effective option for power quality improvement, compensation of the poor power quality effects due to nonlinear loads, or to provide a sinusoidal AC supply to sensitive loads. There are a large number of low-power nonlinear loads in a single-phase power system, such as ovens, air conditioners, fluorescent lamps, TVs, computers, power supplies, printers, copiers, and battery chargers. Low-cost harmonic compensation of these residential nonlinear loads can be achieved using passive filters (Figs. 9.19 and 9.20). Compensation of single-phase high-power traction systems are effectively performed with hybrid filters (Figs. 9.21 and 9.22). Three-phase three-wire power systems are supplying a large number of nonlinear loads with moderate power

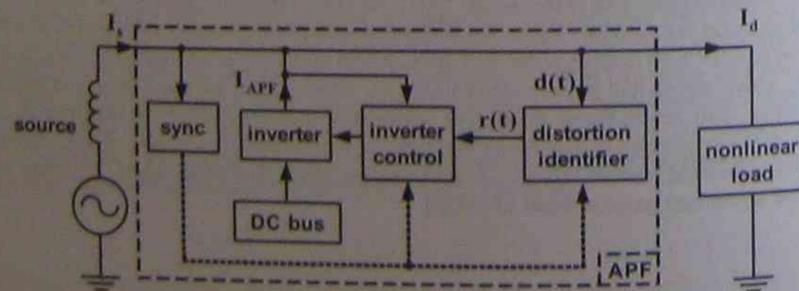


FIGURE 9.26 Control diagram of shunt-connected active power filters (APFs) [6]. For series-connected active filters, the inverter injects the series voltage  $V_{APF}$  via a series-connected transformer. For hybrid filters, two inverters are used for the simultaneous injection of  $I_{APF}$  and  $V_{APF}$ .

levels – such as adjustable-speed drives – up to large power levels associated with HVDC transmission systems. These loads can be compensated using either a group of passive filters (e.g., a passive filter unit as shown in Fig. 9.13a) or a combination of active and passive filters of different configurations (Figs. 9.23 to 9.25) depending on the properties of the AC system.

## 9.6 BLOCK DIAGRAM OF ACTIVE FILTERS

The generalized block diagram of shunt-connected active filters is shown in Fig. 9.26. It consists of the following basic elements [6]:

- **Sensors and transformers** (not shown) are used to measure waveforms and inject compensation signals. Nonsinusoidal voltage and current waveforms are sensed via potential transformers (PTs), current transformers (CTs), Hall-effect sensors, and isolation amplifiers (e.g., optocouplers). Connection transformers in shunt and series with the power system are employed to inject the compensation current ( $I_{APF}$ , see Fig. 9.26) and voltage ( $V_{APF}$ ), respectively.
- **Distortion identifier** is a signal-processing function that takes the measured distorted waveform,  $d(t)$  (e.g., line current or phase voltage) and generates a reference waveform,  $r(t)$ , to reduce the distortion.
- **Inverter** is a power converter (with the corresponding coupling inductance and transformer) that reproduces the reference waveform with appropriate amplitude for shunt ( $I_{APF}$ ) and/or series ( $V_{APF}$ ) active filtering.
- **Inverter controller** is usually a pulse-width modulator with local current control loop to ensure  $I_{APF}$  (and/or  $V_{APF}$ ) tracks  $r(t)$ .

- **Synchronizer** is a signal-processing block (based on phase-lock-loop techniques) to ensure compensation waveforms ( $I_{APF}$  and/or  $V_{APF}$ ) are correctly synchronized with the power system voltage. Certain control methods do not require this block.
- **DC bus** is an energy storage device that supplies the fluctuating instantaneous power demand of the inverter.

The control diagram of the series-connected active filter is identical to that given in Fig. 9.26; however, the inverter injects the series voltage  $V_{APF}$  via a series-connected transformer. For the implementation of hybrid filters, the control diagram of Fig. 9.26 can be expanded to include both shunt ( $I_{APF}$ ) and series ( $V_{APF}$ ) compensation. Detailed implementation and control of a hybrid filter with active shunt and series converters (UPQC) is presented in Chapter 11.

The inverter block represents either a voltage-source inverter (VSI) or a current-source inverter (CSI). The VSI configuration includes an AC inductor  $L_r$  along with optional small AC capacitor  $C_r$  to form a ripple filter (for eliminating the switching ripple and improving the voltage profile) and a self-supporting DC bus with capacitor  $C_d$ . The CSI arrangement uses inductive energy storage at the DC link with current control and the shunt AC capacitors form a filter element. However, VSI structures have more advantages (lower losses, smaller size, less noise, etc.) and are usually preferred. Depending on the supply system, the inverter may be a single-phase two-arm bridge, a three-phase three-arm bridge and a three-phase four-arm bridge, or a mid point or three single-phase (e.g., for a four-wire system) bridge.

The inverter can be connected directly in series with the power system in single phase (to reduce the cost) or through connection transformers (usually with a higher number of turns on the inverter side) to act as a high active impedance blocking harmonic current and representing a low impedance for the fundamental current. In the same manner, the inverter may be connected in shunt either directly to the power system or through step-down transformers to act as an adjustable sink for harmonic currents.

The solid-state switching device is a MOSFET (metal oxide semiconductor field-effect transistor) for low power ratings, an IGBT (insulated-gate bipolar transistor) for medium power ratings, and a GTO (gate turn-off) thyristor for very high power ratings. These switching devices are manufactured in

modular form (with gating, protection, and interfacing elements) to reduce the overall size, cost, and weight.

An essential component of the active filter is the control unit, which consists of a microprocessor. The voltage and current signals are sensed using potential transformers (PTs), current transformers (CTs), Hall-effect sensors, and isolation amplifiers. The control approach (Section 9.7) is implemented online by the microprocessor after receiving input signals through analog-to-digital (A/D) converter channels, phase-lock loop (PLL), and synchronized interrupt signals. All control tasks are carried out concurrently in specially designed processors at a very low cost.

## 9.7 CONTROL OF FILTERS

The initial stage for any filtering process is the selection of the filter configuration. Depending on the nature of the distortion and system structure, as well as the required precision and speed of the compensation, an appropriate filter configuration (e.g., shunt, series, passive, active, or hybrid, as presented in Sections 9.2 to 9.5) is selected. Implementation of passive filters is relatively straightforward, as discussed in Section 9.3. This section presents a classification of control approaches for active and hybrid power filters and identifies their performance strengths.

The control configuration of Fig. 9.26 is open loop because load current  $I_d$  (not supply current  $I_s$ ) is measured, load distortion is identified, and a correction signal is fed-forward to compensate the distortion in the supply current. The open-loop approach has some limitations including inadequate correction (due to errors in calculations and/or inaccuracy in current injection), unstable compensation (e.g., injected current perturbs load and/or source currents such that the distortion is changed), and processing delay (e.g., slow transient response). In contrast, the closed-loop control approach (e.g., measuring the supply current  $I_s$ ) identifies remaining distortion and updates the injected compensation signal.

The choice of control strategy strongly depends on the required compensation response. Active and hybrid filters have the capability to correct a wide range of power quality problems:

- **Harmonic distortion** is taken as a core function of all filter designs. Shunt and series filters are capable of compensating current and voltage distortion, respectively, whereas hybrid filters (with shunt and series components) can correct both current and voltage waveform distortions.

- **Reactive power control** at fundamental frequency is often included in the performance of active filters. It is possible to include harmonic reactive power control with more sophisticated control strategies.
- **Correction of negative- and zero-sequence components** at fundamental frequency due to imbalance and neutral current may be compensated with three-wire and four-wire three-phase hybrid active filters, respectively.
- **Flicker** (e.g., low irregular modulation of power flow) can also be compensated with active filters.
- **Voltage sag and voltage swell** are usually considered to be compensated by a dynamic voltage restorer (DVR), however, sophisticated hybrid active filters such as the UPOC (Fig. 9.21 and Chapter 11) can perform these types of compensations as well.

It is possible to consider and include all various types of power quality problems by adding the corresponding control functions to the basic active filter converter circuit; however, power rating and cost factors will become important and will raise challenging issues, especially in high-power applications.

There are three stages for the implementation of active (or hybrid) power filters (Fig. 9.26) [8]:

- **Stage One: Measurement of Distorted Waveform  $d(t)$ .** For implementation and monitoring of the control algorithm, as well as recording various performance indices (e.g., either both voltage or/and current THDs, power factor, active and reactive power), instantaneous distorted voltage and/or current waveforms need to be measured. This is done using voltage transformers (PTs), current transformers (CTs), or Hall-effect sensors including isolation amplifiers. Measured waveforms are filtered to avoid associated noise problems.
- **Stage Two: Derivation of Reference Signal  $r(t)$ .** Measured distorted waveforms (consisting of fundamental component and distortion) are used to derive the reference signal (e.g., distortion components) for the inverter. This is done by the distortion identifier block. There are three main control approaches for the separation of the reference signal from the measured waveform, as discussed in Sections 9.7.1 to 9.7.3. The selected control method affects the rating and performance of the filter.
- **Stage Three: Generation of Compensation Signal  $i_{ref}$  for  $V_{ref}$ .** The inverter reproduces the refer-

ence waveform with appropriate amplitude for both/either shunt ( $I_{ref}$ ) and/or series ( $V_{ref}$ ) active filtering. These compensation signals are injected into the system to perform the required compensation task. The inverter control block uses reference-following techniques (discussed in Section 9.7.5) to generate the gating signals for the solid-state switches of the inverter.

Shunt active filters are often placed in low-voltage distribution networks, where there is usually a considerable amount of voltage distortion due to the propagation of current harmonics injected by nonlinear loads. Nonsinusoidal voltages at the terminals of an active filter will deteriorate its performance and require additional control functions.

Control objectives of filters are classified based on the supply current components to be compensated and by the response required to correct the distorted system voltage. An important question for the selection of filter control is, what is the most desirable response (of the combined filter and load) to the distortion of the supply voltage? Considering this question, there are three main control categories of compensation (Stage Two, as discussed in Section 9.7.1):

- **Waveform compensation** is based on achieving a sinusoidal supply current. The combination of filter and load is resistive at fundamental frequency and behaves like an open circuit for harmonic frequencies.
- **Instantaneous power compensation** relies on drawing a constant instantaneous three-phase power from the supply. In response to supply harmonic voltages, significant harmonic currents are drawn that result in nonsinusoidal current flow. The combination of filter and load generates a complicated and nonlinear response to the distorted excitation that cannot be described in terms of impedance.
- **Impedance synthesis** responds to voltage distortion with a resistive characteristic and draws harmonic currents in phase with the harmonic voltage excitation. The combination of filter and load draws power at all harmonic frequencies of the supply voltage and can be made to closely approximate a passive system.

There are a variety of reference-following techniques (Stage Three) that can be implemented to generate the compensation signal  $i_{ref}$ , including hysteresis-band, PWM, deadbeat, sliding, and fuzzy control, etc. A number of these control approaches are discussed in Section 9.7.5.

### 9.7.1 Derivation of Reference Signal using Waveform Compensation

The objective of waveform compensation is to achieve a sinusoidal supply current. There are many signal-processing techniques that can be used to decompose the distorted waveform into its fundamental (to be retained) and harmonic (to be cancelled) components. This is essentially a filtering task; however, in addition to the analytical approaches, there are also pattern-learning techniques that may be implemented.

#### 9.7.1.1 Waveform Compensation using Time-Domain Filtering

Distortion identification is a filtering task that can be performed by time-domain techniques or by Fourier-based frequency decomposition. The nonideal properties of real filters such as attenuation (e.g., preserving the identified components and heavily

attenuating other components with a narrow bandwidth), phase distortion (e.g., preserving the phase of the identified components), and time response (e.g., considering the time-varying nature of the distortion signal and enforcing rapid filter response without large overshoot) must be recognized. The performance considerations of time-domain filters are linked, for example, smoothness of the magnitude response has to be traded off versus the phase response, and a well-damped transient response is in conflict with a narrow transition region. There are two general approaches to identify the distortion components in the time domain (Fig. 9.27a):

- **Direct distortion identification** applies a high-pass filter to the distorted signal  $d(t)$  to determine the reference  $r(t)$ . Therefore, the identification process is subject to the transient response of the filter.
- **Indirect distortion identification** uses the filter to determine the fundamental component  $f(t)$  and

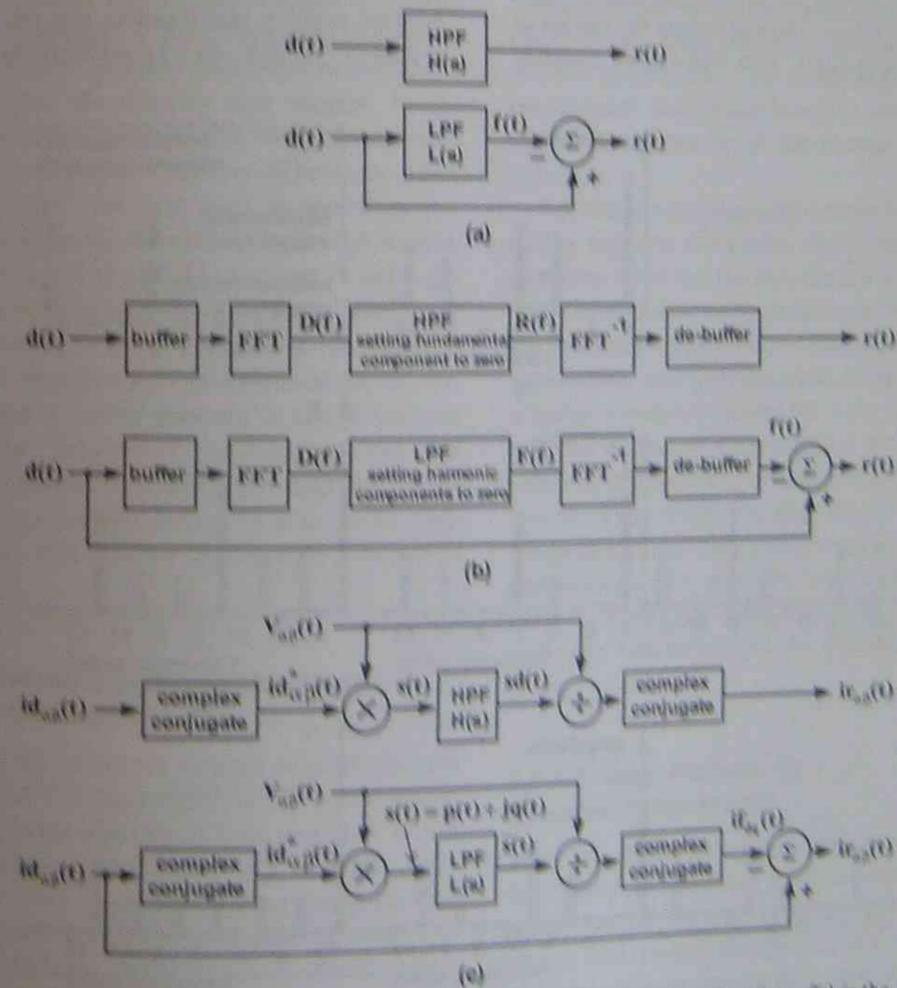


FIGURE 9.27 Direct and indirect distortion identification techniques in (a) time domain, where  $f(t)$  is the identified fundamental frequency signal that is allowed to remain, (b) frequency domain, where  $D(f)$ ,  $R(f)$ , and  $F(f)$  are the frequency-domain representations of distortion, reference, and fundamental component of the distorted signal, respectively [6], (c) instantaneous power domain.

subtracts it from the distorted signal  $d(t)$  to form the reference  $r(t)$ .

Due to the inherent time lag of actual filters, the distortion term of the direct method will be out of date and the distortion cancellation will be in error. The disadvantage of the indirect method is the out-of-date fundamental term that requires additional exchange of real power through the inverter, resulting in DC-bus voltage disturbance and increased rating of the inverter. Most active filters use indirect distortion identification to achieve the best distortion cancellation during transients. Direct methods are preferred in applications where specific ranges of harmonics are to be compensated or where different groups of harmonics are to be treated differently.

To facilitate the separation of fundamental and harmonic components of the signal, active filter control algorithms rely on transformation techniques to transfer the signal from the conventional three-phase (abc) reference frame to an orthogonal two-phase representation. This will reduce the burden of intensive computations. Two well-known transfor-

mations, the stationary  $\alpha\beta 0$  reference and the rotating  $dq0$  reference (also called Park transformation) frames, are widely employed (see Fig. 9.27). The spectra of a nonlinear load current (supplied by the undistorted sinusoidal supply voltage) in abc,  $\alpha\beta 0$ , and  $dq0$  reference frames are shown in Fig. 9.28a,b,c, respectively. Analysis of these graphs indicates:

- The nonlinear load is assumed to be three-wire, three-phase and unbalanced that injects harmonics of the order  $(6k \pm 1)$ , where  $k$  is any positive integer. This is clearly demonstrated by the frequency spectrum in the (abc) phase domain (Fig. 9.28a). Note that there is no distinction between harmonic components of the same order with different phase rotation.
- Both  $\alpha\beta 0$  and  $dq0$  decompositions (Fig. 9.28b,c, respectively) transfer the zero-sequence component into a separate component set. Harmonic components with the same order and opposite phase rotation (e.g.,  $-h$  and  $h$ ) are separated because positive and negative sets are shifted to orders  $(h-1)$  and  $-(h-1)$ , respectively.

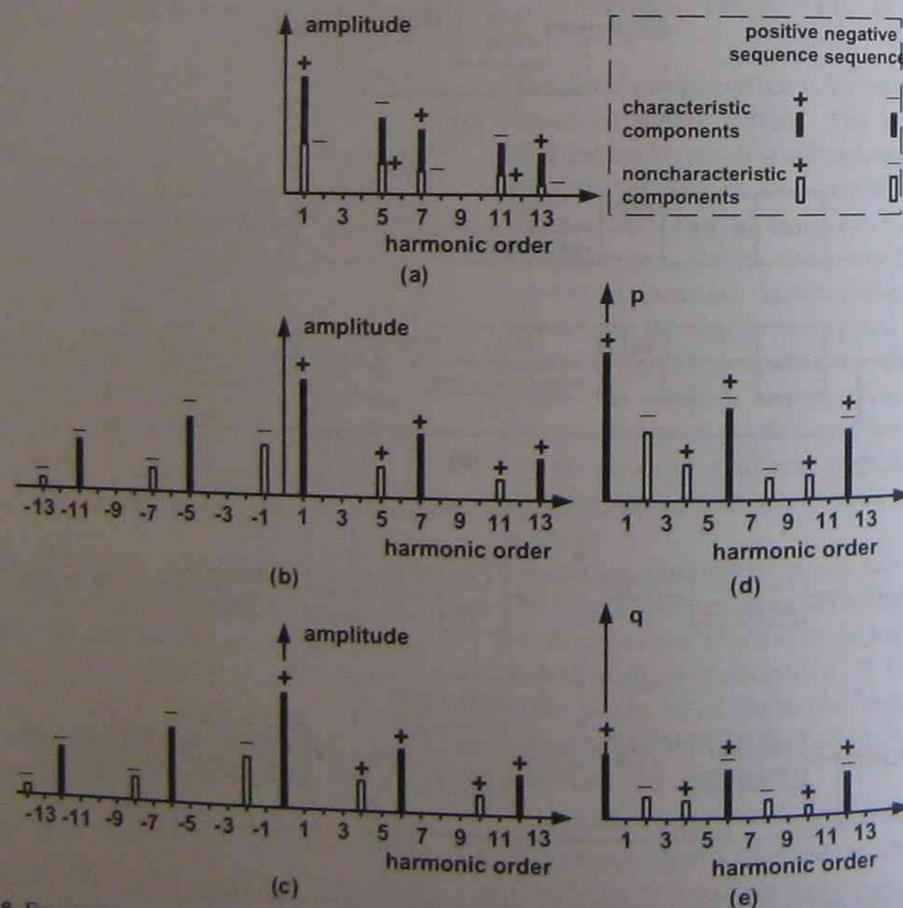


FIGURE 9.28 Frequency spectrum of an unbalanced, three-wire three-phase nonlinear load (injecting current harmonics of order  $h = (6k \pm 1)$ ): (a) current in phase domain, (b) current in  $\alpha\beta 0$  domain, (c) current in  $dq0$  domain, (d) active power (p) in instantaneous power domain, (e) reactive power (q) in instantaneous power domain [6].

- The  $\alpha\beta 0$  transformation (Fig. 9.28b) has no effect on the frequency spectra and does not separate sequence sets. The sequence can be determined from whether either the “ $\alpha$ ” or the “ $\beta$ ” component leads. The negative harmonic term of order  $-1$  indicates the imbalance of the fundamental. Balanced nonlinear loads produce characteristic harmonics of order  $-5, +7, -11, +13, \dots, 6k+1$ . Unbalanced nonlinear loads generate in addition noncharacteristic harmonic components of order  $+5, -7, +11, -13, \dots, 6k-1$ .
- With the rotating  $dq0$  transformation (Fig. 9.28c) all frequency components are shifted downward by one harmonic order. The positive-sequence fundamental becomes a DC term and the negative-sequence fundamental becomes a double-frequency term (order  $-2$ ). The characteristic and noncharacteristic distortions are of orders  $6k$  and  $(6k-2)$ , respectively.
- There is no difference between filtering in the abc or  $\alpha\beta 0$  domains, but the  $dq0$  domain is a better alternative because it offers frequency separation of fundamental, positive, and negative sequences, which makes the filtering task simpler. In the abc domain the fundamental may be separated using a low-pass filter that cuts off between orders 1 and 5 (or 1 and 3 if there is zero-sequence/four-wire harmonic distortion). In the  $dq0$  domain, the filter cutoff should be between 0 and 6 for balanced conditions. For unbalanced conditions, a cutoff between 0 and 2 will allow the negative-sequence (unbalanced) fundamental to be corrected and a cutoff between 2 and 4 will not cancel the unbalanced fundamental but will cancel harmonic distortion. Zero-sequence distortion is conveniently placed in a separate component set that may be cancelled or retained as required.

### 9.7.1.2 Waveform Compensation Using Frequency-Domain Filtering

Filtering in the frequency domain requires discrete or fast Fourier transform (DFT or FFT) on a section of the signal that contains at least one cycle of the lowest frequency of interest and that has been sampled at over twice the highest harmonic frequency as prescribed by the Nyquist theorem. The advantage of filtering in the frequency domain is that completely abrupt cutoffs (with no transition band, low-pass band ripple, and phase distortion) can be obtained. The main disadvantage is that the filtering process is not very suitable for real-time filters and

sufficient time is required for sampling the signal and performing the transformation. In addition, the signals must be steady state and periodic because FFT implicitly assumes periodicity of the sampled waveform. If the FFT window is properly synchronized to the fundamental signal then the phase and magnitudes of the components can be accurately determined. If the sampling window does not cover an integer number of fundamental cycles, accuracy will be degraded (spectral leakage).

Distortion identification may also be performed with a direct or indirect approach using frequency-domain filtering (Fig. 9.27b). FFT is performed to transfer the distorted signal  $d(t)$  to the frequency domain  $D(f)$ . In the direct method, the fundamental component is set to zero to form a cancellation reference. The filter may also cancel the reactive component if only the real (in-phase) component of the signals are set to zero. In the indirect method, all harmonic terms are set to zero; the fundamental is subtracted from the instantaneous signal to generate the reference signal. The filter may also cancel the reactive component if the imaginary (quadrature) fundamental component is set to zero. The final step is the application of the inverse FFT to generate  $r(t)$ .

A problem with frequency-domain filtering is that during transient conditions, the periodicity of the distortion is lost and the cancellation is not accurate. There is also time delay in filtering that can affect the distortion identification performance. For most applications, one complete cycle of data is stored in a buffer, processed during the next cycle, and debuffered for use as a cancellation reference in the following cycle, that is, the cancellation reference is two cycles out of date. For applications requiring fast compensation, shorter update rates are possible by performing a FFT every half-cycle using one half-cycle of fresh data plus data from the previous half-cycle. This will reduce the filtering delay to one cycle.

### 9.7.1.3 Other Methods for Waveform Compensation

There are other waveform compensation schemes that attempt to overcome the disadvantages of time-domain techniques (e.g., compromises or imperfections in filter design) and the inherent time delay of frequency-domain approaches, such as heterodyne methods and neural networks.

The heterodyne methods of waveform compensation involve multiplying the distorted signal by a

sinusoid [6]. If the sinusoid is of fundamental frequency then the fundamental frequency component of the distorted signal will be transformed to DC and double-frequency terms. The DC term can be separated with a low-pass filter. If the heterodyning sinusoid is in phase with the voltage, the fundamental active current is identified; otherwise, the fundamental reactive current can be identified using a quadrature sinusoid. As with the time-domain approaches, a low-order filter provides poor separation of the DC and double-frequency terms and a sharp (high-order) filter will have a long step response. Heterodyne methods of waveform compensation are popular in single-phase systems where  $\alpha\beta 0$  and  $dq0$  transformations are not applicable.

Separation of a signal into the fundamental and distorted components can also be performed by using neural networks [6]. Both direct and indirect principles can be implemented. Neural networks can be used as harmonic identifiers to estimate the Fourier coefficients of the distorted signal. They can be trained to learn the characteristics of the load current (or that of the local grid system) to produce the cancellation reference. They may also be employed to provide fast-frequency decomposition to identify the fundamental component (e.g., for indirect algorithms) or low-order harmonics for a range of load current amplitudes.

### 9.7.2 Derivation of Compensated Signals Using Instantaneous Power Compensation

Another approach to control active filters is to cancel the fluctuating component of instantaneous power and perhaps compensate the fundamental component of the reactive power. A common approach is to start with the definitions of instantaneous active and reactive powers and express them in terms of average and alternating (fluctuating) components. This can be performed in either the  $abc$ ,  $\alpha\beta 0$ , or  $dq0$  domain:

- In the  $\alpha\beta 0$  domain:

$$\begin{bmatrix} v_0 \\ v_\alpha \\ v_\beta \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} & 1/\sqrt{2} \\ 1 & -1/2 & -1/2 \\ 0 & \sqrt{3}/2 & -\sqrt{3}/2 \end{bmatrix} \begin{bmatrix} v_a \\ v_b \\ v_c \end{bmatrix} \quad (9-12)$$

Without the zero-sequence component, the instantaneous power can be written as

$$\begin{aligned} s(t) &= p(t) + jq(t) \\ &= v_{\alpha\beta} i_{\alpha\beta}^* = (v_\alpha + jv_\beta)(i_\alpha - ji_\beta) \\ &= (v_\alpha i_\alpha + v_\beta i_\beta) + j(v_\beta i_\alpha - v_\alpha i_\beta) \end{aligned} \quad (9-13a)$$

where the superscript \* denotes the complex conjugate. Therefore,

$$\begin{bmatrix} p \\ q \end{bmatrix} = \begin{bmatrix} v_\alpha i_\alpha + v_\beta i_\beta \\ v_\beta i_\alpha - v_\alpha i_\beta \end{bmatrix} = \begin{bmatrix} v_\alpha & v_\beta \\ v_\beta & -v_\alpha \end{bmatrix} \begin{bmatrix} i_\alpha \\ i_\beta \end{bmatrix} \quad (9-13b)$$

- In the  $dq0$  domain:

$$\begin{bmatrix} v_d \\ v_q \\ v_0 \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} \cos\theta_d & \cos(\theta_d - 2\pi/3) \\ -\sin\theta_d & -\sin(\theta_d - 2\pi/3) \\ 1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix} \begin{bmatrix} v_a \\ v_b \\ v_c \end{bmatrix} \quad (9-14)$$

In this equation  $\theta_d = \omega_d t + \phi$ , where  $\omega_d$  is the angular velocity of voltages and  $\phi$  is the initial voltage angle. With no zero-sequence components:

$$\begin{aligned} s(t) &= p(t) + jq(t) \\ &= v_{dq} i_{dq}^* = (v_d + jv_q)(i_d - ji_q) \\ &= (v_d i_d + v_q i_q) + j(v_q i_d - v_d i_q) \end{aligned} \quad (9-15)$$

In four-wire systems there is the additional term of zero-sequence instantaneous (real or reactive [6]) power; with Eqs. 9-13 and 9-15 the instantaneous power may be written as

$$\begin{aligned} p(t) &= \bar{p} + \tilde{p}(t) \\ q(t) &= \bar{q} + \tilde{q}(t) \end{aligned} \quad (9-16)$$

Figure 9.28a,d,e shows the spectra of current, active, and reactive powers for the case of a sinusoidal supply voltage, which is harmonically distorted and generates unbalanced currents. Characteristic harmonics of order  $h = 6k + 1$  (e.g., -11, -5, 7, 13, ...) where negative orders represent negative-sequence harmonics) produce power terms of order  $6|k|$ , whereas noncharacteristic harmonics of order  $h = 6k - 1$  (e.g., -13, -7, 5, 11, ...) yield power terms of order  $6|k| \pm 2$ .

The inverse transform (e.g., conversion from power domain to the phase domain) is

$$i_{\alpha\beta}^* = i_\alpha - ji_\beta = \frac{s}{v_{\alpha\beta}} = \frac{(pv_\alpha + qv_\beta) + j(qv_\alpha - pv_\beta)}{v_\alpha^2 + v_\beta^2} \quad (9-17)$$

or

$$\begin{bmatrix} i_\alpha \\ i_\beta \end{bmatrix} = \frac{1}{v_\alpha^2 + v_\beta^2} \begin{bmatrix} v_\alpha & v_\beta \\ v_\beta & -v_\alpha \end{bmatrix} \begin{bmatrix} p \\ q \end{bmatrix} \quad (9-18)$$

Figure 9.27c depicts direct and indirect distortion identification approaches based on the instantaneous power domain as given by Eq. 9-18. The concept is analogous to that of the frequency domain and similar comments apply.

Equation 9-18 assumes sinusoidal supply voltages and distorted currents. However, active filter control relying on the instantaneous power method causes harmonic currents to flow when the supply voltage is either distorted or unbalanced (see Application Examples 9.3 and 9.4). The following comments apply to the instantaneous power decomposition:

- Since  $p$  and  $q$  terms are readily available (e.g., by setting the  $q$ -term to zero in the indirect method and not removing it by filtering in the direct method), it is easy to include the compensation of fundamental reactive power in the active filter control algorithm and perform optimal power follow.
- Fundamental-frequency negative-sequence current appears as a second harmonic in the instantaneous power domain and may be easily filtered.
- The instantaneous power method applied in the  $\alpha\beta 0$  domain has low processing burden because it does not require rotational transformation and explicit synchronization.
- The inverse transformation of Eq. 9-18 assumes sinusoidal supply voltages with current distortions. If both the supply voltage and the load current are distorted, active filter (with instantaneous power compensation) will result in harmonic current flow through the supply (Eq. 9-22). A similar scenario occurs when the supply contains negative-sequence voltages introducing imbalance in the currents and harmonic distortion [6]. Efforts such as modifying the inverse transformation and altering the definition of  $p$  and  $q$  have been made to overcome this problem.
- This section has focused on the control of shunt active filters. Similar discussions apply to the control of series active filters for which dual equations can be generated.

#### 9.7.2.1 Application Example 9.2: Instantaneous Power for Sinusoidal Supply Voltages and Distorted Load Currents

Assuming a sinusoidal supply voltage and a distorted load current (with fundamental and a single harmonic component of order  $h$ ), find the equations for instantaneous power as well as average and fluctuating, pulsating, or oscillating real and reactive powers.

tuating, pulsating, or oscillating real and reactive powers.

**Solution:**

$$\begin{aligned} p(t) &= V_1 I_1 + V_1 I_h \cos[(1-h)\omega t] \\ &\Rightarrow \begin{cases} \bar{p} = V_1 I_1 \\ \tilde{p} = V_1 I_h \cos[(1-h)\omega t] \end{cases} \\ q(t) &= -V_1 I_h \sin[(1-h)\omega t] \Rightarrow \begin{cases} \bar{q} = 0 \\ \tilde{q} = -V_1 I_h \sin[(1-h)\omega t] \end{cases} \end{aligned} \quad (9-19)$$

#### 9.7.2.2 Application Example 9.3: Instantaneous Power Consumed by a Resistive Load Subjected to Distorted Supply Voltages

A three-phase distorted voltage waveform consisting of the fundamental and one harmonic component of order  $h$  is connected across the terminals of a balanced three-phase resistor bank in ungrounded Y configuration. Compute the components of voltages and currents in the  $\alpha\beta 0$  domain and determine the average and the fluctuating active power consumed by the load.

**Solution:**

The load is balanced and has no zero-sequence terms due to the ungrounded Y. The  $\alpha$  and  $\beta$  components are

$$\begin{aligned} v_\alpha &= V^{(1)} \cos(\omega t) + V^{(h)} \cos(h\omega t) \\ v_\beta &= V^{(1)} \sin(\omega t) + V^{(h)} \sin(h\omega t) \\ i_\alpha &= \frac{V^{(1)}}{R} \cos(\omega t) + \frac{V^{(h)}}{R} \cos(h\omega t) \\ i_\beta &= \frac{V^{(1)}}{R} \sin(\omega t) + \frac{V^{(h)}}{R} \sin(h\omega t) \end{aligned} \quad (9-20)$$

Applying Eqs. 9-13 and 9-16:

$$\begin{aligned} p(t) &= (v_\alpha i_\alpha + v_\beta i_\beta) = \bar{p} + \tilde{p}(t) \\ &\Rightarrow \begin{cases} \bar{p} = \frac{(V^{(1)})^2}{R} + \frac{(V^{(h)})^2}{R} \\ \tilde{p}(t) = 2 \frac{V^{(1)} V^{(h)}}{R} \cos[(1-h)\omega t] \end{cases} \end{aligned} \quad (9-21)$$

Note that an oscillatory power with the difference frequency (e.g.,  $(1-h)f_1$ ) is generated. Based on these equations, a nonsinusoidal current must be drawn from a distorted supply voltage to maintain a constant instantaneous power. Similarly, a nonsinusoidal current is required to draw constant instantaneous power as well as average and fluctuating, pulsating, or oscillating real and reactive powers.

neous power from an unbalanced supply voltage (containing a fundamental-frequency negative-sequence component). Therefore, both/either distorted and/or unbalanced supply voltages will force the active filter (with instantaneous power based controller) to inject harmonic currents.

### 9.7.2.3 Application Example 9.4: Supply Current Distortion Caused by Active Filters with Instantaneous Power-Based Controllers

An active filter with an instantaneous power controller is applied to the system of Application Example 9.3. Compute  $\alpha$  and  $\beta$  components of the supply current after the filter has been installed and the nonsinusoidal load current (through the resistive load) has been compensated.

#### Solution:

Relying on Eqs. 9-18 and 9-21, the supply current corresponding to constant power is

$$\begin{aligned} i_{\alpha} &= \frac{pV_{\alpha}}{v_{\alpha}^2 + v_{\beta}^2} \\ &= \frac{p[V^{(1)} \cos(\omega t) + V^{(h)} \cos(h\omega t)]}{(V^{(1)})^2 + 2V^{(1)}V^{(h)} \cos[(1-h)\omega t] + (V^{(h)})^2} \\ i_{\beta} &= \frac{-pV_{\beta}}{v_{\alpha}^2 + v_{\beta}^2} \\ &= \frac{p[V^{(1)} \sin(\omega t) + V^{(h)} \sin(h\omega t)]}{(V^{(1)})^2 + 2V^{(1)}V^{(h)} \cos[(1-h)\omega t] + (V^{(h)})^2} \end{aligned} \quad (9-22)$$

Note the presence of different harmonics in the numerators and denominators which are not of the same order as that of the voltage excitation (e.g., order  $h$ ). Therefore, a single voltage harmonic distortion gives rise to an infinite series of current harmonics when the active filter controller is based on instantaneous power compensation.

### 9.7.3 Derivation of Compensating Signals Using Impedance Synthesis

Impedance synthesis is based on the idea of modifying the inverse transform of the instantaneous power (Eq. 9-17) to prevent injection of higher frequency current harmonics. If Eq. 9-17 is modified using the root-mean-square (rms) value of the current, that is, replace  $v_{\alpha}^2 + v_{\beta}^2$  with  $(v_{\alpha})_{rms} + (v_{\beta})_{rms}$ , the denominator will not be time varying and a modulation of the

current is avoided. There are two impedance synthesis approaches where the voltage and current are related by a chosen value of the impedance: impedance-based blocking and impedance-based compensation.

#### 9.7.3.1 Impedance-Based Blocking

Impedance-based blocking control presents resistive characteristics at all frequencies. A filter arrangement with a number of shunt and series (passive and/or active) branches is used to block or enable a signal path. An inverter acting as an impedance relating voltage to current by a simple transfer function can form one branch of the filter. This normally takes the form of a hybrid filter consisting of active and passive elements, although combinations of active units – without passive elements – are also possible.

There are many forms of hybrid filters (Section 9.5) that can be used for impedance-based blocking. For example, a hybrid combination consisting of a series active filter and a shunt passive filter can be used to perform impedance synthesis. The role of the series branch is to block harmonic currents by representing a high impedance. The instantaneous power theory can be utilized to separate the distortion terms of the current. The active filter then injects a voltage proportional to this current to synthesize a moderately high impedance. In practice, the filter employed to separate the oscillatory terms in the instantaneous power may not be perfect and might influence the impedance presented by the overall active filter [6].

#### 9.7.3.2 Impedance-Based Compensation

A difficulty faced in designing the control of active filters for general purposes (e.g., correcting a group of nonlinear loads) is that the system dynamics are unknown. Furthermore, the compensation current in response to the detected distortion – might activate one of the system resonances or perturb the voltage and cause instability [6].

One solution is to use a shunt device that draws a current proportional to the voltage. This is done by utilizing a dissipative active filter that absorbs energy at harmonic frequencies; thus voltage harmonics are detected and damped. This is a passive controller because it presents a resistive characteristic. Therefore, the operation of the active filter is stable regardless of the system structure.

### 9.7.4 DC Bus Energy Balance

The DC buses of inverters in active power filter systems are not DC links but energy storage devices. If a voltage-source inverter is used, the link contains a capacitor; otherwise an inductor acts as the DC link for the current-source inverter.

In practice, the link voltage will not usually remain constant due to various effects:

- real power exchange between the active filter and the AC grid,
- converter (conduction and switching) losses,
- undesirable real power components in the compensation reference signal due to magnitude and phase errors of the distortion identifier or because of time delays in responding to a transient condition,
- the error between the identified correction current and the actual output current of the inverter that may lead to some power exchange, and
- distortion in the grid voltage that might cause some real power exchange.

To overcome these deficiencies, converter power losses are compensated by drawing a balancing power into the DC bus from the AC grid. This may be performed through a DC-bus voltage regulator (Fig. 9.29) as follows:

- The voltage error signal is generated based on a reference DC voltage;
- The error is passed through a controller;
- A PI compensator operates on the voltage error. It should have a low crossover frequency to avoid interaction with the compensation system;
- Controller output is taken as a demand for fundamental active current and is added to the compensation reference;
- The control algorithm can be implemented in any convenient domain (e.g., abc,  $\alpha\beta 0$ , or  $dq0$  domain); and
- The bandwidth of the controller must be carefully selected: if it is too high (comparable with the

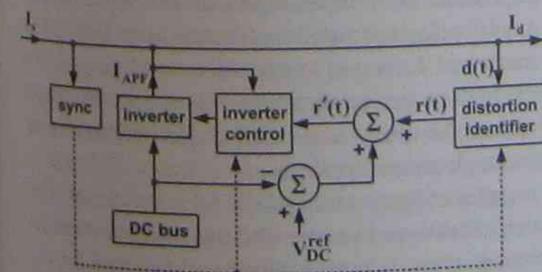


FIGURE 9.29 A simple DC-bus voltage regulator [6].

fundamental frequency), the injected balancing current will contain components at harmonic frequencies that will add distortion to the system; if it is too low, the DC-link voltage may deviate from its nominal value.

### 9.7.5 Generation of Compensation Signal Using Reference-Following Techniques

The identified reference signal (with one of the techniques discussed in Sections 9.7.1 to 9.7.3) must be generated or reproduced by the inverter (Fig. 9.26) and injected into the system to eliminate the power quality problem. Generation of the compensation signal that accurately follows the identified reference may be difficult because of the following:

- the high rate of change and the wide bandwidth of the reference signal,
- the errors in the generated reference caused by the  $di/dt$  limit of a voltage-source inverter,
- the voltage imposed on the inverter (e.g., difference between the available DC-bus voltage and the instantaneous voltage of the AC system),
- the impact of increasing the DC-bus voltage – to improve the reference following – on the ratings of the inverter, and
- the effect of the processing delay on the formation of the reference waveform.

Three approaches to force the inverter output current to follow a reference signal are widely implemented: PWM current regulation, hysteresis regulation, and deadbeat or predictive control.

**PWM Current Regulation.** The current error, for example, the difference between identified (reference) and generated signals, is acted on by a PI controller and its output is passed through a PWM or space-voltage vector modulation to define the voltage to be produced by the inverter. The controller may be of the open- or closed-loop type and can be implemented in any convenient (abc,  $\alpha\beta 0$ , or  $dq0$ ) domain.

**Hysteresis Regulation.** The main idea is to force the compensation signal to follow the reference signal within a given hysteresis band error (e.g.,  $i_{\text{compensation}} = i_{\text{reference}} \pm \Delta i_{\text{hysteresis}}/2$ ). The implementation of this controller is easy as it requires an op-amp operating in the hysteresis mode. Hysteresis regulation is unconditionally stable, does not require detailed plant data, and can achieve high rates of change in the controlled variable. Unfor-

Unfortunately, there are several drawbacks such as the unpredictable switching frequency and the broad-band switching noise injected by the nonconstant switching frequency. Consequently, different approaches have been considered to maintain constant (or near constant) switching frequency and to synchronize the switching of all three phases.

**Deadbeat or Predictive Control.** Deadbeat or predictive control is attractive for following rapidly changing reference signals of active filters because it selects a voltage command for the inverter that will force the generated current to reach a target value by the end of the next sample period [6]. However, it requires knowledge of the system to accurately model the rate of change of current ( $di/dt$ ) and to properly select the voltage command. The interface inductance of the inverter is a key parameter and the opposing AC system voltage must be measured or estimated. Deadbeat controllers may be applied when there is some parameter uncertainty (e.g., the coupling inductor). Adaptive filters can be employed to predict the current reference, and the deadbeat controller can use the predicted current at the end of the sample period as the target current [6].

### 9.7.6 Application Example 9.5: Hybrid of Passive and Active Power Filters for Harmonic Mitigation of Six-Pulse and Twelve-Pulse Rectifier Loads [16]

This example demonstrates the application of hybrid filters to compensate harmonics of a nonlinear load consisting of two six-pulse rectifiers. The two rectifiers are connected to the secondary of a ( $Y/\Delta$ ,  $Y$ ) transformer. The simultaneous operation of the two six-pulse rectifiers represents a twelve-pulse rectifier load. Two arrangements of hybrid filters are considered:

**Hybrid Filter #1** is composed of a shunt-hybrid filter in parallel with a passive filter as shown in Fig. E9.5.1. The passive filter consists of a set of tuned branches. The hybrid power filter is a series combination of an active filter with a small rating (converter) and a passive branch. Due to the use of a parallel passive filter, the converter rating is decreased and the performance and resonance problems of the passive filter are expected to improve.

**Hybrid Filter #2** is composed of a shunt-hybrid filter in parallel with two passive filters tuned at the 5th and 7th harmonics as shown in Fig. E9.5.2. The hybrid filter consists of an active filter with a small rating in series with two passive branches and is tuned at the dominant 11th and 13th harmonics.

- Plot the load current waveforms and calculate  $THD$ , with twelve-pulse and six-pulse rectifier configurations.
- Derive the equations for power system and passive and hybrid filter currents.
- With a six-pulse rectifier load, plot the waveforms of the power system, load, passive filter, and hybrid filter branch currents before and after the installation of hybrid filters #1 and #2.
- Plot the power system current under resonant conditions before and after the addition of hybrid filter #2.
- Compare the performances of hybrid filters #1 and #2.

### 9.8. SUMMARY

With the increase of harmonic currents and voltages in present-day power systems, the installation of passive, active, and hybrid filters gains in importance. In the future, recommended practices such as IEEE-519 [11] will result in further increased use of filters within the distribution system. There are a great variety of filter configurations (Figs. 9.3 and 9.13 to 9.25). Classification of filters can be based on different criteria such as supply type, filter connection, number of filter elements, power rating, compensation type, speed of response, and control technique. In this chapter the classification of power filters is performed based on the type of supply (Fig. 9.3) and the control method (Section 9.7). Proper selection of filter configurations depends primarily on the properties of nonlinear loads, type of supply, and system rating:

- Passive filter blocks (Fig. 9.12 and 9.13) and a combination of passive filters (Figs. 9.19 and 9.20) are the most qualified candidates for single-phase systems – with high penetration of nonlinear loads – and low-power applications.
- Hybrid filters (Figs. 9.21 and 9.22) are considered as a cost-effective option for power quality improvement, compensation of the poor power quality effects of nonlinear loads, or to provide a sinusoidal AC supply to sensitive loads, especially for high-power applications. They are also good options for compensation of single-phase systems and high-power applications.
- A group of passive filters (Fig. 9.13a) or a combination of active and passive filters in different configurations (Figs. 9.23 to 9.25) should be used for the compensation of three-phase three-wire power systems that have a great amount of current or

voltage harmonics due to a large number of small- and moderate-rating nonlinear loads, as well as feeding terminals of HVDC transmission systems.

Selection of the control approach (Sections 9.7.1 to 9.7.3 and 9.7.5) greatly depends on the choice of the control objective, for example, the required waveform of the supply current after compensation. The selection of the domain (e.g., time or frequency) and the reference frame (e.g.,  $dq0$  or  $\alpha\beta0$ ) will affect the computational burden required to implement appropriate filters. All active filters perform harmonic mitigation. However, depending on the selected control strategies, additional forms of compensation (e.g., fundamental reactive power, negative-sequence, zero-sequence, phase balancing, sag, swell, and flicker) can be accommodated within the apparent power rating of an active filter. There exist three different definitions for the control objective:

**First Definition:** Supply currents (after filtering) should contain only fundamental frequency components. This is the main task of active filter controllers using waveform compensation (Section 9.7.1).

**Second Definition:** Supply currents (after filtering) should be such that the instantaneous active power is constant while the instantaneous reactive power is zero. This is performed by active filter controllers that use instantaneous power compensation (Section 9.7.2).

**Third Definition:** Supply currents (after filtering) should be entirely active. This is the main function of active filter controllers using impedance-based compensation (Section 9.7.3).

If the supply voltage is not distorted (with nearly sinusoidal waveform), the following remarks should be considered for the selection of the control method:

- The three aforementioned objective definitions are equivalent and the choice of the control method should be based on the ease of their implementation and their instrumentation requirements.
- Given the harmonic limits provided by relevant guidelines, recommended practices, or standards such as IEEE-519 [11], waveform compensation (first definition) is the most important approach. The techniques for this approach separate the fundamental from the harmonic components. Time-domain filters have the advantage of continuity during transient conditions, whereas frequency-domain filters have a better selectivity under

steady-state conditions. The synchronous  $dq0$  reference frame can ease the filter implementation of three-phase systems at the expense of longer processing time.

- The instantaneous power methods (second definition) are beneficial in three-phase systems due to their ease of filter design without the need for  $dq0$  transformation.
- The active current approaches (third definition) are relatively easy to implement because they require only the identification of the (average) real power. These approaches are implicit in controllers that use the energy balance at the DC bus to identify the desired current.

Further complications regarding the selection of the control method for active filters arise if the supply voltage (before filtering) is distorted. This is the case for most practical power quality problems, for example, when active filters are operating on weak feeders of the distribution network. If the supply voltage is distorted, the following guidelines should also be considered for the selection of the control method:

- Distorted supply voltage may increase the apparent power rating of the active power filter.
- Waveform compensation approaches only draw fundamental current and do not generate extra distortion; however, they will not provide damping of the existing distortion.
- Instantaneous active power methods respond to harmonic supply voltages by introducing additional harmonic currents at other frequencies (Eq. 9-22). In particular, a negative-sequence fundamental voltage will cause these controllers to inject harmonic currents.
- Controllers with impedance-based compensation – resulting in active supply current – represent resistive characteristics at all frequencies, and therefore convert nonlinear loads into linear loads. They inherently provide damping and reduce the propagation of harmonic voltages. However, the design of active filters will have to be coordinated with existing approaches for the damping of network resonances.

Active filters can be designed to perform phase balancing if the exchange of instantaneous power between phases is within their ratings.

- All three control approaches (waveform compensation, instantaneous power compensation, and impedance synthesis) can enforce phase balance-