

ph

THE DIAGRAM SHOWS HOW THE STREAM OF WATER EMERGING FROM A FAUCET NICKS DOWN AS IT FALLS. THE INDICATED CROSS SECTIONAL AREAS ARE $A_0 = 1.2 \text{ cm}^2$ AND $A = 0.35 \text{ cm}^2$. THE TWO LEVELS ARE SEPARATED BY A VERTICAL DISTANCE $h = 45 \text{ mm}$. WHAT IS THE VOLUME FLOW RATE FROM THE TAP?



VOLUME FLOW RATE (R_V)

$$R_V = A_0 U_0$$

$$U_0 = ?$$

$$U^2 = U_0^2 + 2gh$$

$$U_0 = \sqrt{\frac{2gh A^2}{A_0^2 - A^2}}$$

$$U_0 = \sqrt{\frac{2 \times 9.81 \times \frac{45}{1000} \times (0.35)^2}{(1.2)^2 - (0.35)^2}}$$

$$= 0.286 \text{ m/s}$$

$$A_0 U_0 = A U$$

$$R_V = 1.2 \times 28.6 \frac{\text{cm}}{\text{s}}$$

$$= 34 \frac{\text{cm}^3}{\text{s}}$$

ph

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WHERE
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WAVE
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R EMERGING
 INDICATED
 $= 0.35 \text{ cm}^2$
 DISTANCE
 THE TAP?

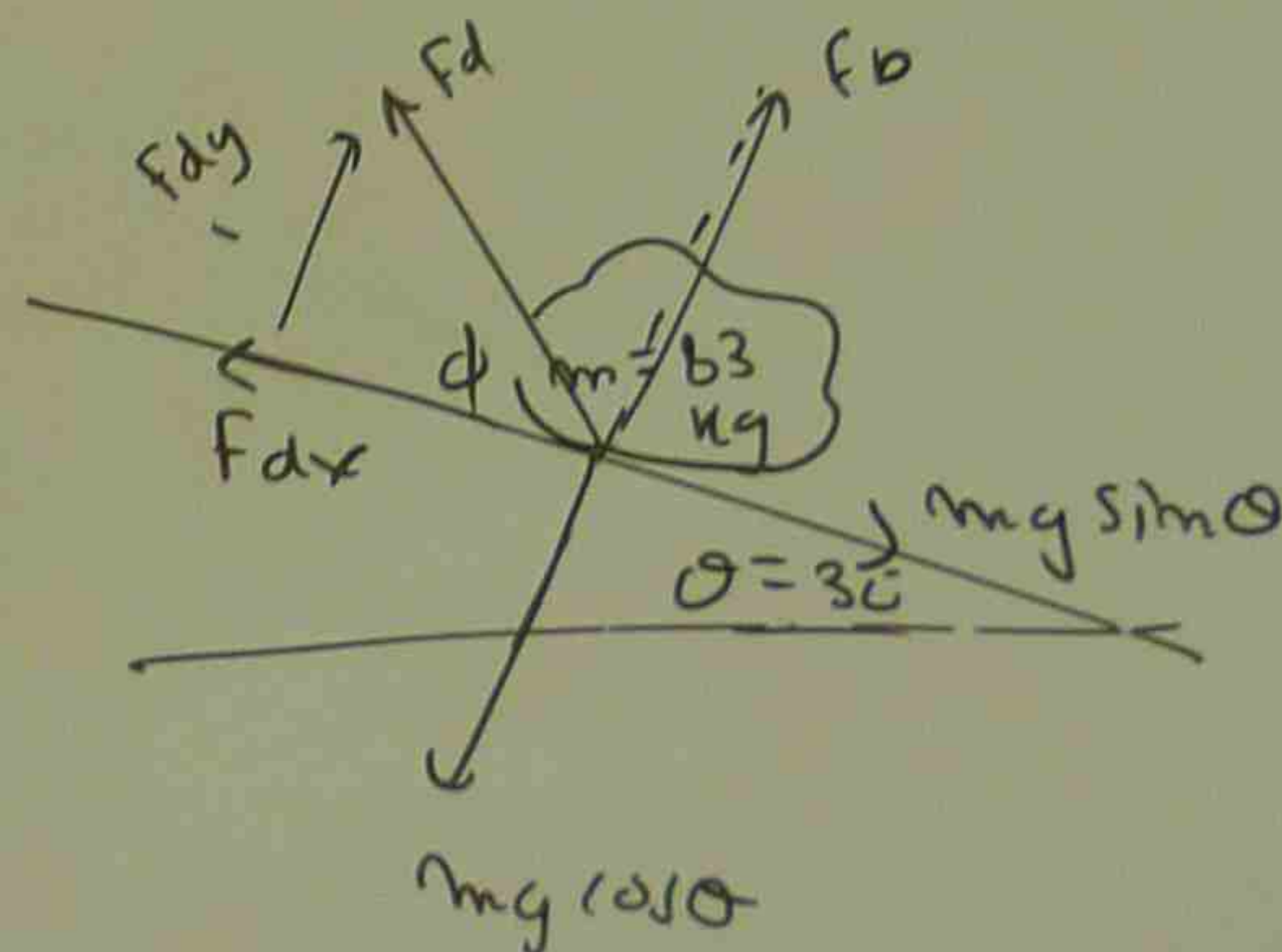
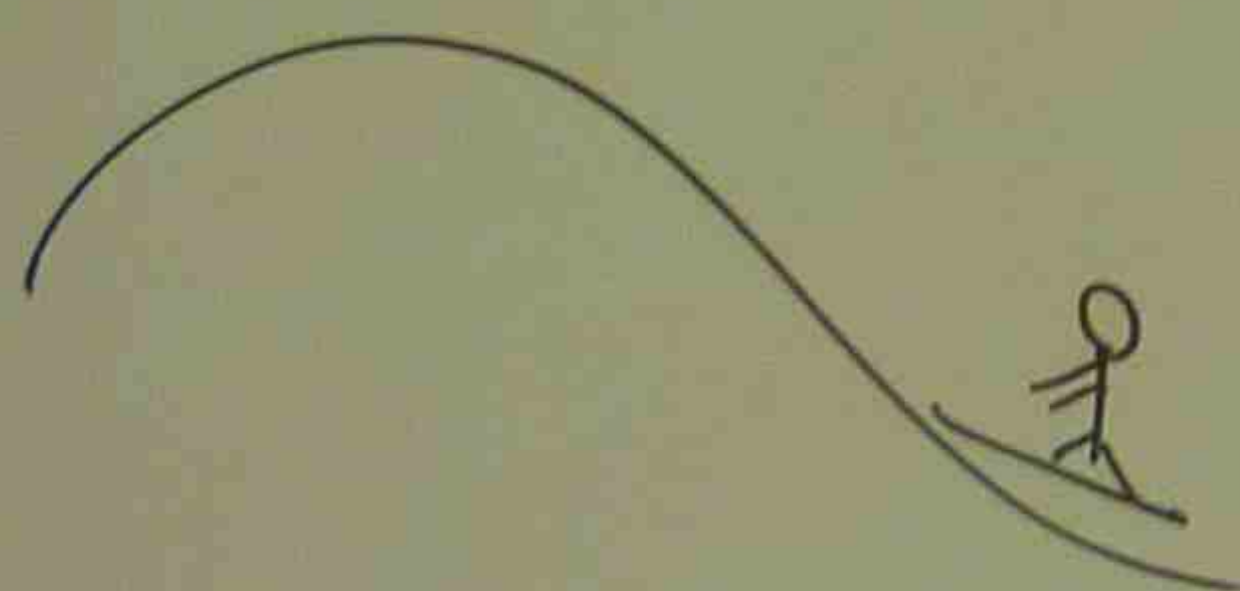
$$R_v = 1.2 \times 28.6 \frac{\text{cm}}{\text{s}} \text{ cm}^2$$

$$= 34 \text{ cm}^3/\text{s}$$

$$(0.35)^2$$

2

ph A SURFER RIDES ON THE FRONT SIDE OF A WAVE AT A POINT WHERE A TANGENT TO THE WAVE HAS A SLOPE OF $\theta = 30^\circ$. THE COMBINED MASS OF SURFER AND SURFBOARD IS $m = 83 \text{ kg}$. THE BOARD HAS A SUBMERGED VOLUME OF $V = 2.5 \times 10^{-2} \text{ m}^3$. THE SURFER MAINTAINS HIS POSITION ON THE WAVE AS THE WAVE MOVES AT CONSTANT SPEED TOWARD SHORE. WHAT ARE THE MAGNITUDE AND DIRECTION OF THE DRAG FORCE ON THE SURFBOARD FROM THE WATER?



$$F_b = \text{water force} = m_f g = \rho V g$$

$$= (1.024 \times 10^3 \text{ kg/m}^3) \times 2.5 \times 10^{-2} \times 9.8 \text{ m/s}^2$$

$$= 2.509 \times 10^2 \text{ N}$$

$$F_{dy} +$$

$$F_{dy} + 2.$$

$$F_d$$

$$F_{dx} =$$

$$=$$

$$=$$

$$F =$$

AT A POINT

$\theta = 30^\circ$

$m = 83 \text{ kg}$

$2.5 \times 10^{-2} \text{ m}^3$

AS THE

DRAW FORCE

$g \sin \theta$

g

$$10^3 \text{ kg/m}^3 \times 2.5 \times 10^{-2} \times 9.8 \text{ m/s}^2$$
$$9 \times 10^2 \text{ N}$$

$$f_{dy} + f_b = mg \cos \theta$$

$$f_{dy} + 2.509 \times 10^2 = 83 \times 9.8 \cos 30$$

$$f_{dy} = 435.5 \text{ N}$$

$$F_{dx} = mg \sin \theta$$

$$= 83 \times 9.81 \sin 30$$

$$= 406.7 \text{ N}$$

$$F = \sqrt{F_{dx}^2 + F_{dy}^2}$$
$$= \sqrt{406.7^2 + 435.5^2}$$
$$= 595.8 \text{ N}$$

THERMAL EXPANSION

LINEAR EXPANSION

$$\Delta L = L \alpha \Delta t$$

L = ORIGINAL LENGTH

α = COEFFICIENT OF LINEAR EXPANSION

Δt = CHANGE OF TEMPERATURE

VOLUME EXPANSION

$$\Delta V = V \beta \Delta t$$

V = ORIGINAL VOLUME

β = COEFFICIENT VOLUMETRIC EXPANSION

$$\beta = 3\alpha$$

AREA EXPANSION

$$\Delta A =$$

$$\gamma =$$

PO on
LOAD

LOAD

WAS 2

How m

Volum

COEFF

Thermal Expansion

Linear Expansion

$$\Delta L = L_0 \alpha \Delta T$$

Original Length

Efficient
Change of

of Linear Expansion
Temperature

Expansion

$$\Delta V = V_0 \beta \Delta T$$

Original

Volume

Efficient
Expansion

Volumetric

$$\beta = 3\alpha$$

Area Expansion

$$\Delta A = A \gamma \Delta T$$

$$\gamma = 2\alpha$$

Q. On a hot day in Las Vegas, an oil tanker loaded 37000 L of diesel fuel. It encounters cold weather on Utah where temperature was 23 K lower than in Las Vegas. How many liters did it deliver?

Volume expansion for diesel fuel is $9.5 \times 10^{-4} / ^\circ\text{C}$
Coefficient of linear expansion is $11 \times 10^{-6} / ^\circ\text{C}$



$$\begin{aligned} \Delta V &= V \beta \Delta T \\ &= (37000 \text{ L}) \times (9.5 \times 10^{-4}) \times (-23) \\ &= -808 \text{ L} \end{aligned}$$

$$\begin{aligned} V_{\text{del}} &= V + \Delta V = 37000 + (-808) \\ &= 36190 \text{ L} \end{aligned}$$

Temperature

Heat is the energy
because of a temperature

$$1 \text{ cal} = 3.7 \text{ J}$$

Heat Absorption

$$\begin{aligned} Q &= C \Delta T \\ C &= m c \end{aligned}$$

$$Q = m$$

Molar specific

Specific heat

mole

TEMPERATURE AND HEAT

HEAT IS THE ENERGY TRANSFERRED BETWEEN A SYSTEM AND ITS ENVIRONMENT.
BECAUSE OF A TEMPERATURE DIFFERENCE THAT EXISTS BETWEEN THEM.

$$1 \text{ cal} = 3.968 \times 10^{-3} \text{ Btu} = 4.1868 \text{ J}$$

HEAT ABSORPTION / HEAT CAPACITY

$$Q = C \Delta T = C (T_f - T_i)$$

$$C = m c$$

c = SPECIFIC HEAT CAPACITY

$$= 4190 \text{ J/kg K}$$

m = MASS (kg)

$$Q = m c \Delta t = m c (T_f - T_i)$$

MOLAR SPECIFIC HEAT

SPECIFYING THE AMOUNT OF SUBSTANCE

mole (mol)

$1 \text{ mol} = 6.02 \times 10^{23}$ ELEMENTARY UNITS

HEAT OF TRANSFORMATION

SOLID \rightarrow LIQUID
ice \rightarrow 0°C

LIQUID \rightarrow LIQUID
0°C \rightarrow 100°C

AMOUNT OF HEAT REQUIRED TO CHANGE THE STATE \rightarrow LATENT HEAT

Ph How much HEAT must be added to a mass $m = 720 \text{ g}$ AT -10°C TO CHANGE STATE AT 15°C ?

I (ICE)

$-10^\circ\text{C ICE} \rightarrow 0^\circ\text{C ICE}$

CHANGE OF TEMPERATURE

\downarrow HEAT ABSORBED

$$Q_1 = m_{\text{ice}} \times c_{\text{ice}} \times \Delta T$$

(WATER)

II CHANGE OF TEMPERATURE

$$Q_2 = m_{\text{WATER}} \times c_{\text{WATER}} \times \Delta T$$

A SYSTEM AND ITS ENVIRONMENT.

WHAT EXISTS BETWEEN THEM.

68 J

HEAT OF TRANSFORMATION

SOLID \rightarrow LIQUID
0°C 0°C

LIQUID \rightarrow VAPOR
100°C 100°C

AMOUNT OF HEAT REQUIRED FOR CHANGING
THE STATE \rightarrow LATENT HEAT.

Pb How much HEAT must be absorbed by ICE of
mass $m = 720$ g. AT -10°C TO TAKE THE LIQUID
STATE AT 15°C ? (ICE) \rightarrow (WATER)

I (ICE)

$-10^\circ\text{C ICE} \rightarrow 0^\circ\text{C ICE}$

CHANGE OF TEMPERATURE

\downarrow
HEAT ABSORBED

$$Q_1 = m_{\text{ICE}} \times C_{\text{ICE}} \times \Delta t$$

(WATER)

II CHANGE OF TEMPERATURE

$$Q_3 = m_{\text{WATER}} C_{\text{WATER}} \Delta t$$

II CHANGE OF
STATE
 $0^\circ\text{C ICE} \rightarrow 0^\circ\text{C WATER}$

$$Q_2 = m_{\text{ICE}} L$$

$$Q_t = Q_1 + Q_2 + Q_3$$

$$= m_{\text{ICE}} C_{\text{ICE}} \Delta t + m_{\text{ICE}} L + m_{\text{WATER}} C_{\text{WATER}} \Delta t$$

$$= \frac{720}{1000} \text{ kg} \times 2220 \frac{\text{J}}{\text{kg}} \times (0 - (-10))$$

$$+ \frac{720}{1000} (333 \text{ kJ/kg})$$

$$+ \frac{720}{1000} \times 4190 \frac{\text{J}}{\text{kg}} \times (15 - 0)$$

$$= 300 \text{ kJ}$$

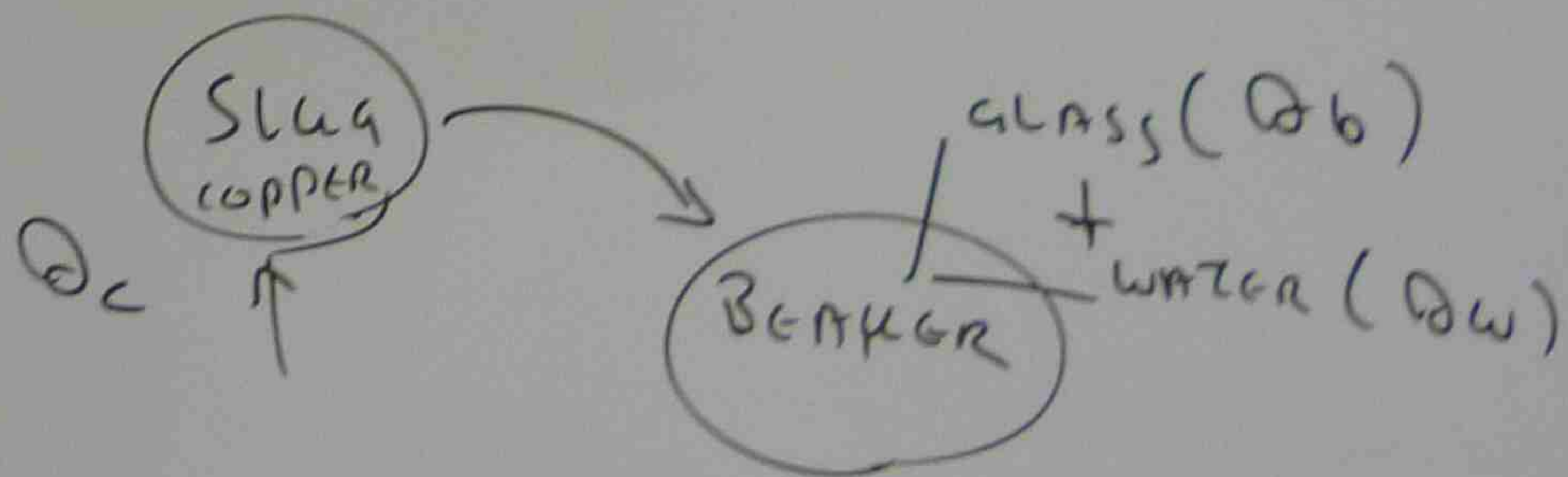
(T_i)

TANCE

2×10^{23} ELEMENTARY
UNITS

pm

A COPPER SLUG WHOSE MASS m_c IS 75 g IS HEATED IN A LABORATORY OVEN TO A TEMPERATURE T OF 312°C . THE SLUG IS THEN DROPPED INTO A GLASS BEAKER CONTAINING MASS $m_w = 220\text{ g}$ OF WATER. THE HEAT CAPACITY C_b OF THE BEAKER IS 45 cal/K . THE INITIAL TEMPERATURE T_i OF THE WATER AND THE BEAKER IS 12°C . ASSUMING THAT THE SLUG, BEAKER AND WATER ARE AN ISOLATED SYSTEM AND THE WATER DOES NOT VAPORIZE. FIND THE FINAL TEMPERATURE T_f OF THE SYSTEM AT THERMAL EQUILIBRIUM.



$$Q_w + Q_b + Q_c = 0$$

$$Q_w = C_w m$$

$$Q_b = C_b$$

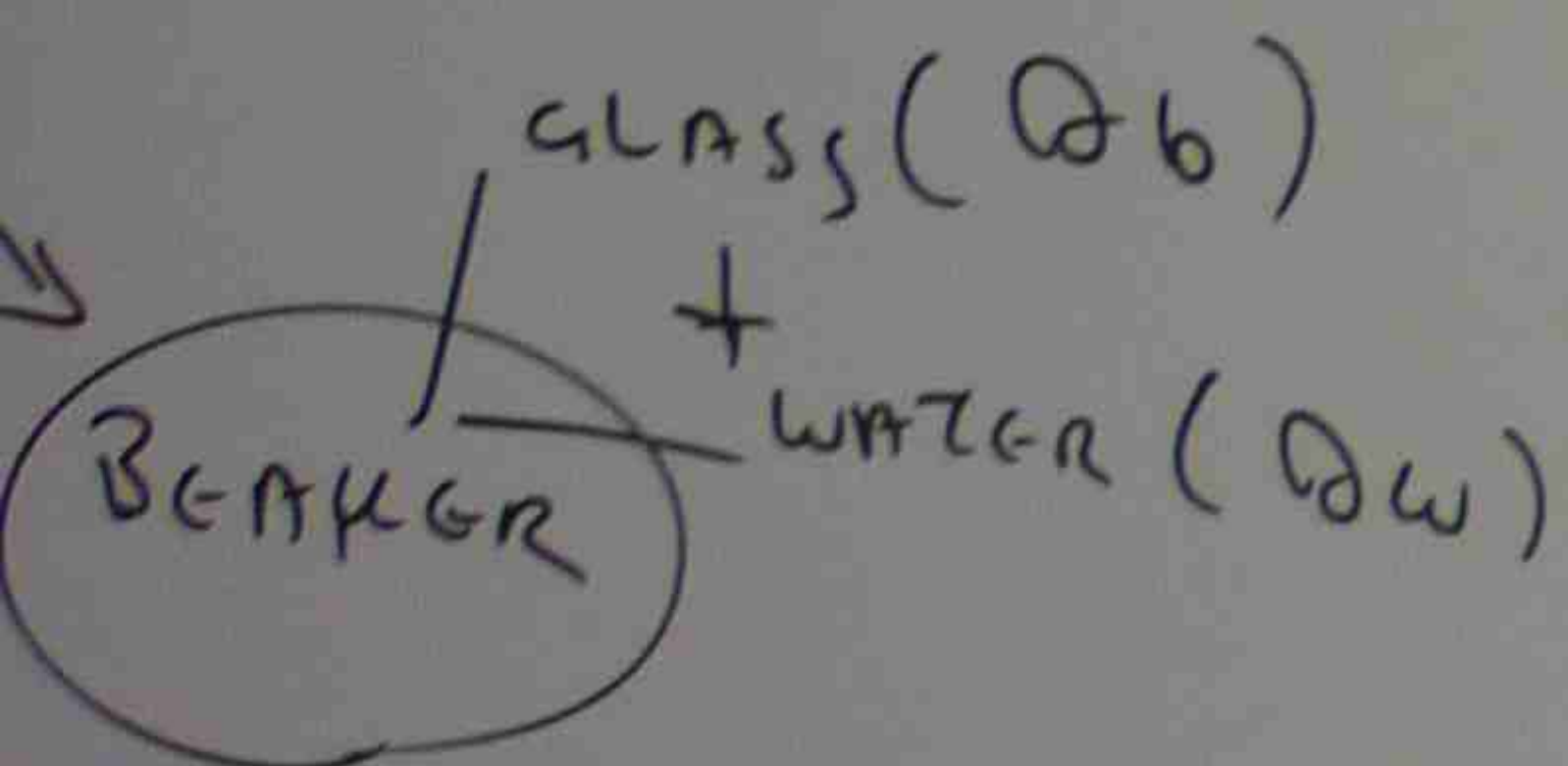
$$Q_c = C_c$$

$$T_f = \frac{C_c}{\dots}$$

$$= \frac{0.0}{1.0}$$

mass m_c is 75 g is
 ly oven to a temperature
 then dropped into a glass
 $m_w = 220$ g of water.
 of the beaker is 45 cal/K

ture T_i of the water and
 assuming that the slug,
 are an isolated system and
 vaporize. Find the final
 of the system at thermal



$$Q_b + Q_c = 0$$

$$Q_w = c_w m_w (T_f - T_i)$$

$$Q_b = C_b (T_f - T_i)$$

$$Q_c = c_c m_c (T_f - T_i)$$

$$T_f = \frac{c_c m_c T + C_b T_i + c_w m_w T_i}{c_w m_w + C_b + c_c m_c}$$

$$= \frac{0.0923 \times 75 \text{ g} \times 312 + 45 \times 12 + 1.00 \times 220 \text{ g} \times 12^\circ \text{C}}{1.00 \times 220 + 45 + 0.0923 \times 75}$$

$$= 20^\circ \text{C} \quad \text{X}$$

GAS

$$PV = nRT$$

K = BOLTZMAN

MR =

$$PV =$$

WORK DONE

$$U_1 \rightarrow U_2$$

INITIAL U

GASES

$$PV = nRT$$

P = PRESSURE

V = VOLUME

R = GAS CONSTANT

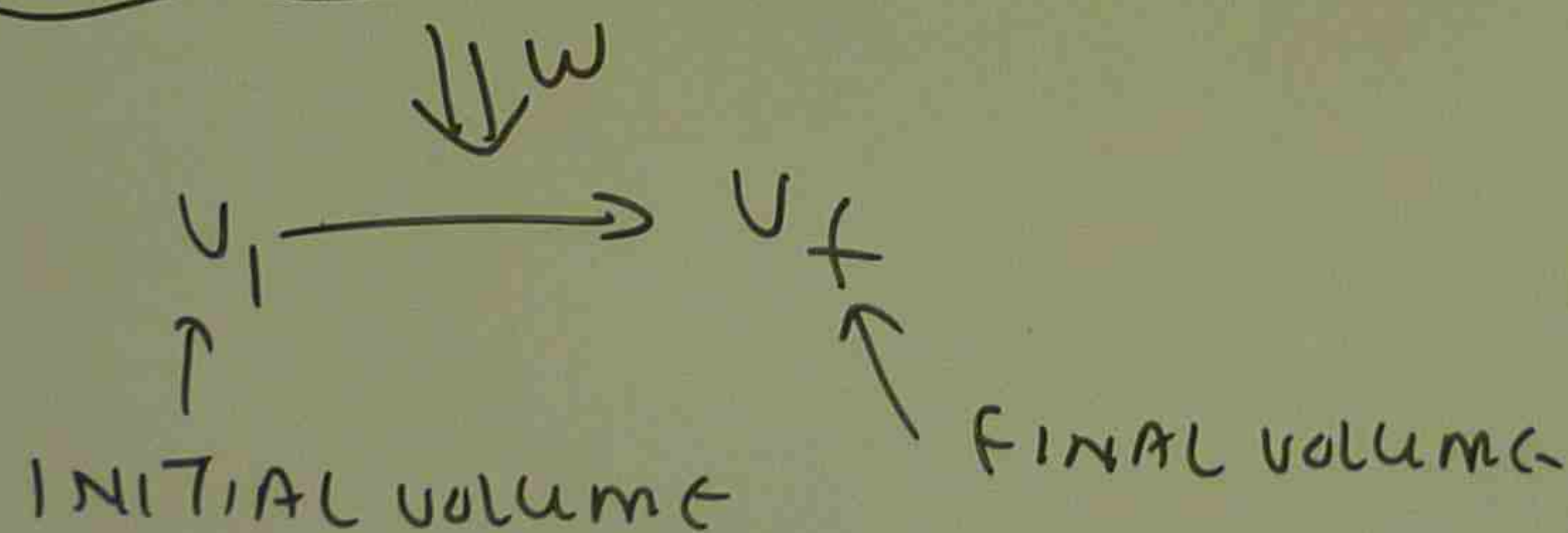
T = TEMPERATURE

$$k = \text{BOLTZMANN CONSTANT} = \frac{R}{N} = \frac{8.31 \text{ J/mol}\cdot\text{K}}{6.02 \times 10^{23} \text{ mol}^{-1}} = 1.38 \times 10^{-23} \text{ J/K}$$

$$nR = Nk$$

$$PV = NkT$$

WORK DONE BY THE GAS AT CONSTANT TEMPERATURE



$$W = nRT \ln \frac{V_f}{V_i} \quad (\text{J})$$

ph A CYLINDER
THE TEMPERATURE
8.5 L. WHAT IS

$$PV = nRT$$

$$\frac{PV}{T} = \frac{nR}{\text{CONSTANT}}$$

pb ONE MOLE OF
310 K FROM AN
 V_f OF 19 L.

URE

$$k = 1.38 \times 10^{-23} \text{ J/K}$$

TEMPERATURE

$$RT \ln \frac{V_f}{V_i}$$

ph A CYLINDER CONTAINS 12 L OF OXYGEN AT 20°C AND IS atm. THE TEMPERATURE IS RAISED TO 35°C AND THE VOLUME IS REDUCED TO 8.5 L. WHAT IS THE FINAL PRESSURE OF THE GAS IN ATMOSPHERE

$$PV = nRT$$

$$\frac{PV}{T} = \frac{nR}{\text{CONSTANT}}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{1 \text{ atm} \times 12}{(20 + 273)} = \frac{P_2 \times 8.5}{(35 + 273)} \rightarrow P_2 = 22 \text{ atm}$$

pb ONE MOLE OF OXYGEN EXPANDS AT A CONSTANT TEMPERATURE T OF 310 K FROM AN INITIAL VOLUME V_i OF 12 L TO A FINAL VOLUME V_f OF 19 L. HOW MUCH WORK IS DONE BY THE GAS DURING EXPANSION?



$$\begin{aligned} W &= nRT \ln \frac{V_f}{V_i} \\ &= (1 \text{ mol}) \times 8.31 \text{ J/mol} \cdot \text{K} \times 310 \ln \frac{19}{12} \\ &= 1180 \text{ J} \end{aligned}$$

ph THE mo

(a) WHAT

(b) WHAT

(c) WHAT

(a) $V_{\text{avg}} = \int$

(b) V_{Rm}

(c) $V_P =$

at 20°C and 1 atm.
The volume is reduced to
gas in atmosphere

$$P_2 = 22 \text{ atm}$$

Temperature T of
L to a final volume
the gas during expansion?

$$T \ln \frac{V_f}{V_i} \\ \times 8.31 \text{ J/mol} \cdot \text{K} \times 310 \ln \frac{19}{12}$$

30 J

pn) THE MOLAR MASS M OF OXYGEN IS 0.0320 kg/mol
(a) WHAT IS THE AVERAGE SPEED V_{avg} OF OXYGEN GAS MOLECULES AT $T = 300^\circ\text{K}$.
(b) WHAT IS THE ROOT MEAN SQUARE SPEED OF V_{rms} AT 300°K .
(c) WHAT IS THE MOST PROBABLE SPEED V_p AT 300°K ?

$$(a) V_{avg} = \sqrt{\frac{8RT}{\pi M}} = \sqrt{\frac{8 \times 8.31 \text{ J/mol} \cdot \text{K} \times 300}{3.1416 \times 0.0320}} = 445 \text{ m/s}$$

$$(b) V_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3 \times 8.31 \times 300}{0.0320}} = 483 \text{ m/s}$$

$$(c) V_p = \sqrt{\frac{2RT}{M}} = \sqrt{\frac{2 \times 8.31 \times 300}{0.0320}} = 395 \text{ m/s}$$

GEN IS 0.0320 kg/mol

OF OXYGEN GAS MOLECULES AT $T = 300^\circ \text{K}$.

RE SPEED OF V_{rms} AT 300°K .

SPEED UP AT 300°K ?

$$\frac{8.31 \text{ J/mol}^\circ \text{K} \times 300}{16 \times 0.0320} = 445 \text{ m/s}$$

$$\frac{5 \times 8.31 \times 300}{0.0320} = 483 \text{ m/s}$$

$$\frac{5 \times 8.31 \times 300}{0.0320} = 395 \text{ m/s}$$

THE MOLAR SPECIFIC HEAT OF IDEAL GAS

INTERNAL ENERGY

$$E_{\text{int}} = \frac{3}{2} n RT$$