



$$e_g = \omega_a \phi \sin \omega t$$

$$\phi = \phi_a + \phi_{res}$$

$$\phi_a = \omega_a i_a$$

$$\begin{aligned} e_g &= \omega_a (\omega_a i_a + \phi_{res}) \sin \omega t \\ &= \omega_a \omega_a i_a \sin \omega t + \omega_a \phi_{res} \sin \omega t \\ &= \omega_a \omega_a i_a \sin \omega t + \omega_a \phi_{res} \sin \omega t \end{aligned}$$

$$E_g = \omega_a \omega_a i_a \sin \omega t + \omega_a \phi_{res} \sin \omega t$$

$$\begin{aligned} \text{developed torque } T &= K_a \phi i_a \\ t &\propto \omega_a \phi i_a^2 \end{aligned}$$

$$\begin{aligned} \text{Average torque } T &= K_a \omega_a i_a^2 \text{ average} \\ &= K_a \omega_a i_a^2 \end{aligned}$$

$$I_{ar} = \text{rms armature current}$$

$$V_a = R_a i_a + L_a \frac{di_a}{dt} + E_g$$

$$E_g = R_a I_a + E_g$$

$$E_g = \frac{2\pi}{\omega} \omega_a \omega_a i_a \sin \omega t = R_a I_a + \omega_a \omega_a i_a \sin \omega t + \omega_a \phi_{res} \sin \omega t$$