

Half wave thyristor with resistance load

$\alpha = \text{firing angle}$

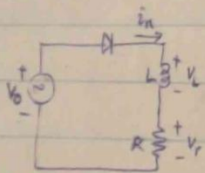
$$V_n = \frac{1}{2\pi} \int_{\alpha}^{\pi} V_0 \sin \omega t \, d(\omega t)$$

$$= 0.225 V_0 (1 + \cos \alpha)$$

$$I_n = \frac{V_0}{R_n} \left[\frac{1}{\pi} \left[\frac{\omega t}{2} + \frac{\sin 2\omega t}{4} \right]_{\alpha}^{\pi} \right]^{\frac{1}{2}}$$

$$= \frac{V_0}{R_n} \left[\frac{1}{2} - \frac{\alpha}{2\pi} - \frac{\sin 2\alpha}{4} \right]^{\frac{1}{2}}$$

3.2 Single phase rectifies reactive load



$\beta = \text{extinction angle}$

Half wave diode with RL load

$$i_1(\omega t) = \frac{\sqrt{2} V_0}{(R^2 + X^2)^{\frac{1}{2}}} \sin(\omega t - \phi)$$

$$\phi = \tan^{-1} \frac{X}{R}$$

$$X = \omega L$$

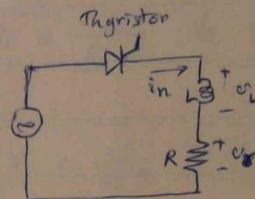
$$i_2(\omega t) = -I_1(\omega t) e^{-t/\tau}$$

$$\tau = \frac{L}{R}$$

$$i_1(\omega t) = \frac{\sqrt{2} V_0}{(R^2 + X^2)^{\frac{1}{2}}} \sin(\omega t - \phi)$$

$$i_n(\omega t) = i_1(\omega t) + i_2(\omega t)$$

$$I_n = \frac{1}{2\pi R} \int_0^{\pi} \sqrt{2} V_0 \sin \omega t \, d(\omega t)$$



Controlled rectifier with RL load

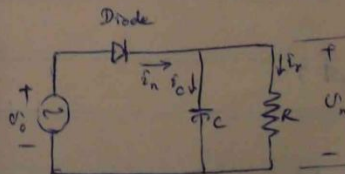
$$i_1(\omega t) = \frac{\sqrt{2} V_0}{(R^2 + X^2)^{\frac{1}{2}}} \sin(\omega t - \phi)$$

$$\phi = \tan^{-1} \frac{X}{R}$$

$$i_2(\omega t) = -i_1(\alpha) e^{-t/\tau}$$

$$i_1(\alpha) = \frac{\sqrt{2} V_0}{(R^2 + X^2)^{\frac{1}{2}}} \sin(\alpha - \phi)$$

$$I_n = \frac{1}{2\pi R} \int_{\alpha}^{\beta} \sqrt{2} V_0 \sin \omega t \, d(\omega t)$$



Half-wave rectifier with parallel RC load